## Supplementary material for Interpretable deep Gaussian processes with moments

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## 1 Second moment for SC[NuN]

Following Eq. (15) in the main text, the second moment for the two-layer DGP is given by,

$$\frac{\sigma_2^2}{2} \left\{ 1 + \exp[2e^{(-\alpha||\mathbf{x}_i||^2 + 2\beta\mathbf{x}_i \cdot \mathbf{x}_j - \alpha||\mathbf{x}_j||^2)} - e^{-2(\alpha - \beta)||\mathbf{x}_i||^2} - e^{-2(\alpha - \beta)||\mathbf{x}_j||^2}] \right\}$$
(1)

where we have suppressed the factor of  $\sigma_1^2/2\ell_2^2$  inside the bracket for convenience.

## 2 Experiments on two UCI datasets

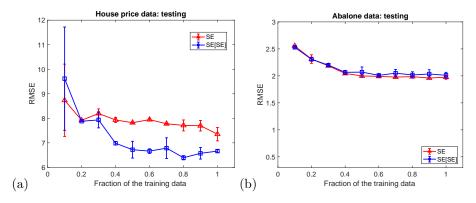
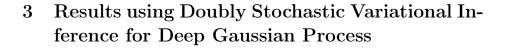


Figure 1: Simulated regression using UCI data sets. House Price data has a total of 320 training and 94 testing data points. Abalone data has a total of 400 training and 400 testing data points.



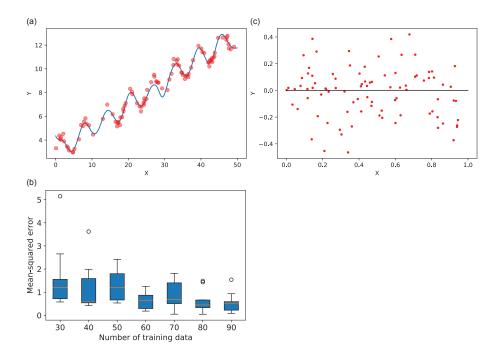


Figure 2: Fit result using the method proposed by Salimbeni and Deisenroth (2017) (https://github.com/ICL-SML/Doubly-Stochastic-DGP). Panels (a), (b), and (c) correspond to Figure 1 (e), (f), and (g), respectively. Because of the existence of outliers, we used boxplots instead of mean  $\pm$ se for the mean-square error in panel (b).

## References

Salimbeni, H. and Deisenroth, M. (2017). Doubly stochastic variational inference for deep gaussian processes. In Advances in Neural Information Processing Systems.