Abstract

Modern deep neural networks require a significant amount of computing time and power to train and deploy, which limits their usage on edge devices. Inspired by the iterative weight pruning in the Lottery Ticket Hypothesis (Frankle & Carbin, 2018), we propose DropNet, an iterative pruning method which prunes nodes/filters to reduce network complexity. DropNet iteratively removes nodes/filters with the lowest average post-activation value across all training samples. Empirically, we show that DropNet is robust across diverse scenarios, including MLPs and CNNs using the MNIST, CIFAR-10 and Tiny ImageNet datasets. We show that up to 90% of the nodes/filters can be removed without any significant loss of accuracy. The final pruned network performs well even with reinitialization of the weights and biases. DropNet also has similar accuracy to an oracle which greedily removes nodes/filters one at a time to minimise training loss, highlighting its effectiveness.

1. Introduction

The surprising effectiveness of neural networks in domains such as image recognition in ImageNet (Russakovsky et al., 2015) has inspired much recent research. Current state-of-the-art deep models include Transformers (Vaswani et al., 2017) for language modelling, InceptionNet (Szegedy et al., 2015) for image modelling, and ResNets (He et al., 2016) which include over 100 layers. In fact, the number of configurable parameters per model has risen significantly from hundreds to tens of millions. The increased computational complexity required for modern neural networks has made deployment on edge devices challenging.

Previous Work on Complexity Reduction: Current methods of reducing complexity include quantization to 16-bit (Gupta et al., 2015), group L1 or L2 regularization (Alemu et al., 2019), node pruning (Castellano et al., 1997; Zhang & Qiao, 2010; Alvarez & Salzmann, 2016; Wen et al., 2016), filter pruning for CNNs (Li et al., 2016; Wen et al., 2016; Alvarez & Salzmann, 2016; He et al., 2017; Liu et al., 2017), weight pruning using magnitude-based methods (Han et al., 2015) or second-order Hessian-based methods such as Optimal Brain Damage (LeCun et al., 1990) or Optimal Brain Surgeon (Hassibi et al., 1993).

Previous Work on Node/Filter Pruning: For node pruning, previous work includes introducing regularization terms based on input weights using group lasso to the loss function (Alvarez & Salzmann, 2016; Wen et al., 2016) and selecting the least important node to drop based on mutual information (Zhang & Qiao, 2010). In CNNs, previous work includes layer-wise pruning such as layer-wise lasso regression on filters (He et al., 2017), and global pruning methods such as pruning filters with the lowest sum of absolute input weights globally (Li et al., 2016), using second-order Taylor expansion to prune unimportant filters (Molchanov et al., 2016; Lin et al., 2018), introducing structured sparsity using a particle filter approach (Anwar et al., 2017), or to repeatedly perform an L1 regularization of the batch normalization layer’s scaling factor in CNNs (Liu et al., 2017).

Previous Work on Iterative Pruning: Most techniques that can perform one-shot pruning can also be applied recursively using iterative pruning. It has been shown that iterative pruning achieves better performance than one-shot pruning (Li et al., 2016). More notably, iterative pruning with reinitialization can reduce parameter counts by over 90% (Frankle & Carbin, 2018). Such iterative pruning methods shed new insight into how more effective pruning approaches might be developed.

Comparison with Similar Work: DropNet iteratively removes nodes/filters with the lowest average post-activation values across all training samples. Similar work to ours includes removing nodes with the highest average percentage of zero activation values across a validation set - Average Percentage of Zeros (APoZ) (Hu et al., 2016), which measures sparsity of a node’s activations. In contrast, DropNet (i) utilizes average magnitude of post-activation values, and
(ii) does so over the training set. Another similar metric is to prune channels to a filter using variance of post-activation values (Polyak & Wolf, 2015). DropNet instead prunes the entire filter using average post-activation values.

**Comparison with Dropout:** Dropout (Srivastava et al., 2014) randomly drops a fraction $p$ of nodes during training, but keeps the entire network intact during test time. DropNet, however, drops nodes/filters permanently during training time and test time.

**Our Contributions:**
- We propose DropNet, an iterative node/filter pruning approach with reinitialization, which iteratively removes nodes/filters with the lowest average post-activation value across all training samples (either layer-wise or globally) and, hence, reduces network complexity. To the best of our knowledge, our method is the first to prune both MLPs and CNNs based on the average post-activation values of nodes/filters, which utilizes both the information about the input weights as well as the input data to make an informed selection of the nodes/filters to drop.
- DropNet achieves a robust performance across a wide range of scenarios compared to several benchmark metrics. DropNet achieves similar performance to an oracle which greedily removes nodes/filters one at a time to minimise training loss.
- DropNet does not require special initialization of weights and biases (unlike (Frankle & Carbin, 2018)). It is shown in subsequent experiments that a random initialization of the pruned model will do just as well as original initialization. This means the architecture pruned by DropNet can be readily deployed using off-the-shelf machine learning libraries and hardware.

**2. DropNet Algorithm**

In this section, we describe the DropNet algorithm and discuss its properties.

Similar to the Lottery Ticket Hypothesis (Frankle & Carbin, 2018), which iteratively drops weights with reinitialization, DropNet applies iterative dropping for nodes/filters with reinitialization.

**Model:** Consider a dense feed-forward neural network $f(x; n)$ with initial configuration of weights and biases $\theta = \theta_0$ and initial configuration of nodes/filters $n$. Let $f$ reach minimum validation loss $l$ with test accuracy $a$ when optimizing with stochastic gradient descent (SGD) on a training set. Consider also training $f(x; m \odot n)$ with a mask $m \in \{0, 1\}^{|n|}$ on its nodes/filters such that its initialization is $f(x; m \odot n)$, where $m \odot n$ is an element-wise multiplication between $m$ and $n$. Let $f$ with the mask reach minimum validation loss $l'$ with test accuracy $a'$.

**Algorithm 1 Iterative Pruning Algorithm**

**Input:** Neural network with initial state $\theta_0$, initial nodes/filters $n$, pruning metric.

**Hyperparameters:** Training iterations $j$, pruning fraction $p \in (0, 1]$, maximum loss factor $\kappa \in (0, 1]$.

**Initialize** starting mask $m = \{1\}^{|n|}$

**repeat**

1. Revert network to initial state $\theta_0$
2. Apply mask to nodes/filters: $f(x; m \odot n)$
3. Train network for at most $j$ iterations until early stopping
4. Apply pruning metric to choose a fraction $p$ of nodes/filters to drop and update $m$

**until** validation accuracy $a' \leq \kappa a$

Run steps 1 to 3

**Problem:** Find a subnetwork $f(x; m \odot n)$ such that $a' \approx a$ (similar accuracy) and $|m|_0 \ll n$ (fewer parameters).

**Algorithm:** The proposed iterative pruning algorithm is shown in Algorithm 1. DropNet applies Algorithm 1 with the following metric: the lowest average post-activation value across all training samples (either layer-wise or globally). An example of the training cycle using Algorithm 1 is shown in Fig. 1.

**Expected Absolute Value of a Node:** Unlike weights, which can be of the same value for all training samples, nodes will change their post-activation values according to the input training samples. Hence, we use a node’s expected absolute value across all training samples $(x_1, x_2, ..., x_t)$ to evaluate its importance. For each node $a_i$, $i \in \mathbb{Z}^+$, $1 \leq i \leq n$, out of all $n$ nodes in the network, we have its expected absolute value as:

$$E(a_i) = \frac{1}{t} \sum_{j=1}^{t} |V(a_i|x_j)|,$$
where $V(a_i|x_j)$ is the post-activation value of the node $a_i$ with input sequence $x_j$.

**Expected Absolute Value of a Filter:** For CNNs, the filters are comprised of a set of constituent nodes. Choosing which filter to drop is thus equivalent to choosing a set of constituent nodes to drop. Hence, in order to evaluate the importances of each filter $f_i$, $i \in \mathbb{Z}^+$, $1 \leq i \leq n$, out of all $n$ filters in the network, we take the average of the expected absolute value of all its constituent nodes $a_1, a_2, ..., a_r$, $r \in \mathbb{Z}^+$. That is:

$$E(f_i) = \frac{1}{r} \sum_{j=1}^{r} |E(a_j)|,$$

where $E(f_i)$ is the expected absolute value of the filter $f_i$ across all training samples $x_1, x_2, ..., x_t$.

**Intuition:** We propose two reasons for the competitiveness of dropping nodes/filters with lowest average post-activation value across all training samples. i) Firstly, Rectified Linear Unit (ReLU) activation will lead to inactive nodes which do not “fire” once the value of node reaches 0 or below. Hence, if a node does not fire most of the time, it will have a low expected absolute value and removing it will affect only a small amount of classifications when its post-activation value is non-zero. (ii) Secondly, during backpropagation, the input weights of a node with low expected absolute value will be updated by only a small amount, which means that the node is less adaptive to learning from the inputs. Removing these less adaptive nodes should impact classification accuracy less than removing more adaptive ones.

### 3. Methodology

In order to evaluate the effectiveness of the DropNet algorithm, we test it empirically using MLPs and CNNs on MNIST (LeCun et al., 2010), CIFAR-10 (Krizhevsky et al., 2009) and Tiny ImageNet (taken from https://tiny-imagenet.herokuapp.com, results in Supplementary Material) datasets.

#### 3.1. Pruning Metrics

The pruning metrics we consider are listed in Table 1. At the end of each training cycle in Algorithm 1, we use the metric to evaluate the importance score for each node/filter, and drop the nodes/filters with the lowest importance scores. Note that ties are broken randomly.

The minimum, maximum and random metrics prune a fraction $p$ of nodes/filters globally. The minimum metric drops a fraction $p$ the nodes/filters globally with the lowest post-activation values. The maximum metric serves as a comparison to the minimum metric to compare the effectiveness of the metric. The random metric, which prunes a fraction $p$ of nodes randomly, serves as a control.

We consider layer-wise pruning metrics. These metrics are termed minimum_layer, maximum_layer and random_layer, and they prune a fraction $p$ of nodes/filters layer-wise.

**DropNet** utilizes Algorithm 1 with either the minimum or minimum_layer metrics. As will be shown in our experimental results, these metrics prove to be quite competitive for different scenarios.

#### 3.2. Experiment Details

**Train-Validation-Test Split:** For MNIST, the dataset is split into 54000 training, 6000 validation and 10000 testing samples. For CIFAR-10, the dataset is split into 45000 training, 5000 validation and 10000 testing samples.

**Pre-processing:** The input pixel values are scaled to be between 0 and 1.

**Activation Function:** The model activation functions are all ReLU, except the final classification layer where it is softmax in order to choose one out of multiple classes.

**Optimization Function:** The optimization function used is SGD with a learning rate of 0.1.

**Loss Function:** The loss function used is cross entropy.

**Training Runs:** The experiments are repeated over 15 runs, each with a different initial random seed. To serve as comparison between the various metrics, the average accuracy against the fraction of nodes/filters remaining across all 15 runs are plotted, together with the error bars denoting the 95% confidence interval.

**Training Cycles:** The masks are applied at the start of each training cycle, which comprises 100 epochs, with early stopping using validation loss with patience of 5 epochs. Over each training cycle, a fraction $p = 0.2$ of the nodes are dropped.

#### 3.3. Model Details

The experiments are performed on a variety of network models. We use three types of feed-forward architectures: two fully-connected (FC) hidden layers of nodes (Model A),

### Table 1. Pruning Metrics

<table>
<thead>
<tr>
<th>Metric</th>
<th>Importance Score</th>
<th>Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>minimum</td>
<td>$E(a_i)$ or $E(f_i)$</td>
<td>GLOBAL</td>
</tr>
<tr>
<td>maximum</td>
<td>$-E(a_i)$ or $-E(f_i)$</td>
<td>GLOBAL</td>
</tr>
<tr>
<td>random</td>
<td>0</td>
<td>GLOBAL</td>
</tr>
<tr>
<td>minimum_layer</td>
<td>$E(a_i)$ or $E(f_i)$</td>
<td>LAYER-WISE</td>
</tr>
<tr>
<td>maximum_layer</td>
<td>$-E(a_i)$ or $-E(f_i)$</td>
<td>LAYER-WISE</td>
</tr>
<tr>
<td>random_layer</td>
<td>0</td>
<td>LAYER-WISE</td>
</tr>
</tbody>
</table>
Figure 2. Models of the neural network architectures considered. Varying numbers of initial hidden nodes/filters are used in different experiments, but the baseline architectures remain the same. The layers where the masks are applied are written with a postfix ‘[Mask]’, and shown in orange. The CNN models (Model B and C) are variants of the VGG architecture (Simonyan & Zisserman, 2014). Model A: FC40 - FC40 (Left): This is a network with two fully-connected (FC) hidden layers, each with 40 nodes. The mask is applied after each hidden layer. Model B: Conv64 - Conv64 (Middle): This is a network with a two 2D convolutional layers each comprising of 64 filters of size 3x3 with ‘same’ padding. The mask is applied after the convolutional layer and before the MaxPooling2D layer. Model C: Conv64 - Conv64 - Conv128 - Conv128 (Right): This is a network with a four 2D convolutional layers. The first two convolutional layers have 64 filters, while the next two convolutional layers have 128 filters. The filter is of size 3x3 with ‘same’ padding. The mask is applied after the convolutional layer and before the MaxPooling2D layer.

4. Results

4.1. MLP - MNIST

Q1. Can DropNet perform robustly well on MLPs of various starting configurations?

To address this question, we conduct the experiments on different versions of Model A on MNIST, listed as follows:

1.1) Model A: FC40 - FC40. The plot of test accuracy against fraction of nodes remaining for various metrics is shown in Fig. 3.

1.2) Model A: FC20 - FC40. The plot of test accuracy against fraction of nodes remaining for various metrics is shown in Fig. 4.

1.3) Model A: FC40 - FC20. The plot of test accuracy against fraction of nodes remaining for various metrics is shown in Fig. 5.

As the trends for training, validation, and test accuracies are similar, we only show the plots for test accuracy.

For 1.1), it can be seen (Fig. 3) that the minimum layer performs the best, followed closely by minimum, then random layer, maximum layer, random and lastly maximum. The maximum metric performs poorly when the fraction of nodes remaining is 0.5 and below.

For 1.2), it can be seen (Fig. 4) that the minimum metric performs the best, followed by the layer-wise and random metrics, and lastly the maximum metric.

For 1.3), it can be seen (Fig. 5) that the minimum and minimum layer are both competitive, followed by random layer, random, maximum layer, and lastly maximum metric. minimum performs well for all fractions of nodes remaining except between 0.1 and 0.3 where minimum layer performs slightly better. The maximum metric can be seen to be consistently poor when the fraction of nodes remaining is 0.6 and below.

Evaluation: The results indicate that, for fully connected networks, when the hidden layer sizes are equal (i.e., no bottleneck layer), the minimum layer metric is competitive. When the hidden layer sizes are unequal (i.e., there potentially exists a bottleneck layer), the minimum metric is competitive. This shows that minimum and minimum layer
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Figure 3. Test accuracy vs. fraction of nodes remaining for various metrics in Model A: FC40 - FC40 on MNIST

Figure 4. Test accuracy vs. fraction of nodes remaining for various metrics in Model A: FC20 - FC40 on MNIST

Figure 5. Test accuracy vs. fraction of nodes remaining for various metrics in Model A: FC40 - FC20 on MNIST

Figure 6. Test accuracy vs. fraction of filters remaining for various metrics in Model B: Conv64 - Conv64 on MNIST

Figure 7. Test accuracy vs. fraction of filters remaining for various metrics in Model B: Conv32 - Conv64 on MNIST

Figure 8. Test accuracy vs. fraction of filters remaining for various metrics in Model B: Conv64 - Conv32 on MNIST

are competitive metrics for Model A. Using DropNet, we are able to reduce the number of nodes by 60% or more without significantly affecting model accuracy, highlighting its effectiveness in reducing network complexity.

4.2. CNN - MNIST

Q2. Can DropNet perform robustly well on CNNs of various starting configurations?

To address this question, we conduct experiments on different versions of Model B on MNIST, listed as follows:

2.1) **Model B: Conv64 - Conv64**. The plot of test accuracy against fraction of filters remaining for various metrics is shown in Fig. 6.

2.2) **Model B: Conv32 - Conv64**. The plot of test accuracy against fraction of filters remaining for various metrics is shown in Fig. 7.

2.3) **Model B: Conv64 - Conv32**. The plot of test accuracy against fraction of filters remaining for various metrics is shown in Fig. 8.

As the trends for training, validation, and test accuracies are similar, we only show the plots for test accuracy.

For 2.1), it can be seen (Fig. 6) that the minimum_layer metric performs the best, followed by random_layer, minimum, random, maximum_layer, and lastly maximum metric. The maximum metric can be seen to be consistently poor when the fraction of filters remaining is 0.3 and below.

For 2.2), it can be seen (Fig. 7) that the minimum metric performs the best, followed by minimum_layer, random_layer, random, maximum_layer, and lastly maximum metric. The maximum metric can be seen to be consistently poor when the fraction of filters remaining is 0.5 and below. The random metric is in between the performance of the minimum and maximum metrics.

For 2.3), it can be seen (Fig. 8) that the minimum metric performs the best, followed by minimum_layer, random, random_layer, maximum_layer, and lastly maximum metric. The maximum metric can be seen to be consistently poor when the fraction of filters remaining is 0.2 and below. The performance of the random metrics is in between the performance of the minimum and maximum metrics.

**Evaluation:** The findings are similar to Section 4.1. The results indicate that for convolutional layers, when the hidden layer sizes are equal (i.e., no bottleneck layer), the minimum_layer metric is competitive. When the hidden layer sizes are unequal (i.e., there potentially exists a bottleneck layer), the minimum metric is competitive. This shows that minimum and minimum_layer are competitive metrics for Model B. Using DropNet, we are able to reduce the number of filters by 90% or more without...
significantly affecting model accuracy, highlighting its effectiveness in reducing network complexity.

4.3. CNN - CIFAR-10: Model C

Q3. Can DropNet perform well on a larger dataset like CIFAR-10?

To address this question, we conduct an experiment using Model C on CIFAR-10, listed as follows:

3.1) Model C: Conv64 - Conv64 - Conv128 - Conv128.

The plot of test accuracy against fraction of filters remaining for various metrics are shown in Fig 9.

3.2) Model C: Conv128 - Conv128 - Conv256 - Conv256.

The plot of training accuracy and test accuracy against fraction of filters remaining for various metrics are shown in Fig. 10.

As the trends for training, validation, and test accuracies are similar, we only show the plots for test accuracy.

It can be seen (Figs. 9 and 10) that the minimum_layer metric performs the best, followed by minimum, random_layer, random, and maximum_layer and lastly maximum metric. The minimum and minimum_layer perform equally well when the fraction of filters remaining is 0.5 and above. The maximum metric can be seen to be consistently poor when the fraction of filters remaining is 0.5 and below. The random metric is in between the minimum and maximum metrics.

Evaluation: The results show that minimum and minimum_layer are both competitive when less than of half of the filters are dropped. Thereafter, minimum_layer performs significantly better. Using DropNet, we can reduce the number of filters by 50% or more without significantly affecting model accuracy, highlighting its effectiveness in reducing network complexity.

The results indicate that, for larger convolutional models like Model C, global pruning methods like the minimum metric may not be as competitive as layer-wise pruning methods like the minimum_layer metric.

4.4. CNN - CIFAR-10: ResNet18/VGG19

Q4. Can DropNet perform robustly well on even larger models such as ResNet18 and VGG19?

To address this question, we conduct an experiment using Algorithm 1 for ResNet18 and VGG19 on CIFAR-10, both following closely to the implementation in their respective papers (Simonyan & Zisserman, 2014; He et al., 2016). Details of the model are in the Supplementary Material. Of note, ResNet18 is implemented without Batch Normalization, while VGG19 had a Batch Normalization before every MaxPooling2D layer.

The plot of test accuracy against fraction of filters remaining for various metrics for ResNet18 and VGG19 is shown in Figs. 11 and 12 respectively.

For ResNet18, it can be seen (Fig. 11) that the minimum_layer metric performs the best, followed by minimum, then random_layer, random, maximum_layer and and lastly maximum metric. The minimum_layer and minimum are both competitive.

For VGG19, it can be seen (Fig. 12) that the minimum_layer metric performs the best, followed by random_layer, random, max_layer, minimum, and and lastly maximum metric. The minimum_layer metric is the most competitive.

For both ResNet18 and VGG19, the maximum metric can be seen to be consistently poor when the fraction of filters remaining is 0.5 and below. The maximum_layer metric is consistently poor when the fraction of filters remaining is 0.2 and below.

Evaluation: The results show that for larger models, minimum_layer is the most competitive. It can also be seen that with the exception of minimum and maximum_layer, the layer-wise metrics outperform the global metrics for larger models. This shows that there may be significant statistical differences between layers for larger models such that comparing magnitudes across layers may not be a good way to prune nodes/filters. That said, minimum_layer can be seen to perform very well and consistently performs better than random, which shows promise that it is a good metric.

The minimum metric proves to be almost as competitive as minimum_layer for ResNet18, but performs worse than random for VGG19. This shows that the skip connections in ResNet18 help to alleviate some of the pitfalls of global metrics. Interestingly, the minimum metric tends to prune out some skip connections completely, which shows that certain skip connections are unnecessary. This means that DropNet using the minimum metric is able to automatically identify these redundant connections on its own.

Overall, using DropNet, we can reduce the number of filters by 80% or more without significantly affecting model accuracy, highlighting its effectiveness in reducing network complexity even in larger models.

5. Empirical Analysis - Oracle Comparison

Q5. How competitive is the DropNet algorithm compared to an oracle?

There are numerous node/filter pruning methods and algorithms available, hence, rather than comparing the performance of DropNet with these individual methods and
algorithms, we utilize an oracle in order to establish the competitiveness of DropNet. We define the oracle as the algorithm which greedily drops a node/filter out of all remaining node/filters available at every iteration of Algorithm 1 such that the overall training loss is minimized. In order to provide a fair comparison with the oracle, nodes/filters are also pruned one at a time when using the various metrics.

In order to perform a “stress” test on the various metrics compared to the oracle, we analyze their performance on a smaller scale model, listed as follows:

5.1) **Model A: FC20 - FC20.** The plot of test accuracy against fraction of nodes remaining when compared against an oracle on MNIST is shown in Fig. 13.

5.2) **Model B: Conv20 - Conv20.** The plot of test accuracy against fraction of filters remaining when compared against an oracle on MNIST is shown in Fig. 14.

For 5.1), it can be seen (Fig. 13) that the oracle performs the best, followed closely by minimum, then random and lastly maximum metrics. The random metric used here is actually the random_layer metric, as it provides a stronger baseline performance. Although not shown, minimum_layer has similar performance to minimum.

For 5.2), it can be seen (Fig. 14) that the oracle, minimum and random perform equally well. The worst performing is the maximum metric, with poor performance with 0.4 or less fraction of filters remaining.

**Evaluation:** The results indicate that overall, the minimum metric is competitive even to an oracle which minimizes training loss. This shows that the minimum metric is indeed a competitive criterion to drop nodes/filters.

We note that Algorithm 1 with a pruning metric runs in linear time. The oracle runs in polynomial time, as it has to iterate through all possible node/filter selections at the end of each iteration of Algorithm 1.
6. Empirical Analysis - Random Initialization

**Q6. Is the starting initialization of weights and biases important?**

We compare the performance of a network retaining its initial weights and biases $\theta_0$ when performing iterative node/filter pruning, as compared to a network with the pruned architecture but with a random initialization ($\text{random init}$). We conduct the following experiments:

6.1) **Model A: FC20 - FC20.** The plot of test accuracy against fraction of nodes remaining for original and random initialization is shown in Fig. 15.

6.2) **Model B: Conv64 - Conv64.** The plot of test accuracy against fraction of filters remaining for original and random initialization is shown in Fig. 16.

6.3) **Model C: Conv64 - Conv64 - Conv128 - Conv128.** The plot of test accuracy against fraction of filters remaining for original and random initialization is shown in Fig. 17.

It can be seen (Figs. 15, 16, and 17) that unlike the Lottery Ticket Hypothesis (see Figure 4 in (Frankle & Carbin, 2018)), DropNet does not suffer from loss of performance when randomly initialized for up to 70% to 80% of the nodes/filters being dropped.

**Evaluation:** This means that for DropNet, only the final pruned network architecture is important, and not the initial weights and biases of the network. One reason that the original initialization is not important may be because the learning rate is high enough (0.1) for the network to retrain sufficiently given just the model architecture. This concurs with the finding that the 'winning ticket' in the Lottery Ticket Hypothesis does not confer significant advantages over random reinitialization if a larger learning rate of 0.1 is used instead of 0.01 (Liu et al., 2018).

Similar results are also obtained for larger models such as ResNet18 and VGG19 (details in Supplementary Material), which shows that this finding is a general one.

7. Empirical Analysis - Percentage of nodes/filters to Drop

**Q7. Can we drop more nodes/filters at a time to reduce number of training cycles and prune the model faster without affecting accuracy?**
We explore this question by analyzing the performance of the minimum metric. We compare the performance of the model using different values of the pruning fraction $p = 0.2, 0.3, 0.4, 0.5$ and $0.9$. The experiments performed are as follows:

7.1 Model A: FC20 - FC20. The plot of test accuracy against fraction of nodes remaining for various pruning fractions $p$ on MNIST is shown in Fig. 18.

7.2 Model B: Conv64 - Conv64. The plot of test accuracy against fraction of filters remaining for various pruning fractions $p$ on MNIST is shown in Fig. 19.

7.3 Model C: Conv64 - Conv64 - Conv128 - Conv128. The plot of test accuracy against fraction of nodes remaining for various pruning fractions $p$ on CIFAR-10 is shown in Fig. 20.

Evaluation: Overall, it can be seen (Figs. 18, 19, and 20) that dropping a greater fraction $p$ of nodes/filters per training cycle leads to poorer performance. For one-shot pruning methods which attempt to remove 90% of nodes/filters, it is not ideal as it generally leads to worse performance. This further reinforces the competitiveness of iterative pruning as compared to one-shot pruning.

The results also show that larger $p$ has similar performance when dropping up to 70% of the nodes/filters. Hence, it may be possible to iterate faster through Algorithm 1 by adopting a larger $p$ under certain conditions. Further experiments need to be done to determine the optimal pruning fraction $p$, but $p = 0.2$ seems to be competitive.

8. Concluding Remarks

Reflections: In this paper, we propose DropNet, which iteratively drops nodes/filters and, hence, reduces network complexity. We illustrate how DropNet can potentially reduce network size by up to 90% without any significant loss of accuracy. Also, there does not need to be a particular initialization required when dropping up to 70% of the nodes/filters. DropNet also has similar performance to an oracle which greedily removes nodes/filters one at a time to minimise training loss, which shows its competitiveness.

DropNet, utilizing either the minimum or minimum_layer metric, proves to be competitive over a variety of model architectures. The minimum metric seems to work robustly well for smaller models such as Models A and B, while the minimum_layer metric appears to be better for larger models such as Model C, ResNet18 and VGG19, in the configurations we considered.

We conjecture that one reason for the better performance of the minimum_layer metric in larger models is that as the number of layers increases, the statistical properties of the post-activation values of the nodes/filters may be significantly different in each layer. Hence, using a single metric to prune globally may not be as good as pruning layer-wise. The exception is when using skip connections, as empirical results suggest that the minimum metric is also competitive for larger models for ResNet18. This seems to suggest that skip connections work well with DropNet.

Additional Experiments: In our Supplementary Material, we show that DropNet is scalable and achieves similar results on Tiny ImageNet. Furthermore, we also compare DropNet with another data-driven approach, APoZ, and show that DropNet outperforms APoZ and can achieve better test accuracy for the same amount of pruning.

Future Work: To further show DropNet's generalizability, more experiments can be done on i) alternative neural network architectures such as RNNs, as well as ii) other domains such as NLP and reinforcement learning. DropNet has been shown to work well empirically with ReLU activation functions, and it remains to be seen whether other metrics may be required for other activation functions such as sigmoid, tanh and ReLU variants.

Source Code: To encourage further research on iterative pruning techniques, the source code used for our experiments is publicly available at https://github.com/tanchongmin/DropNet.
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