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# Meta-Learning Neural Bloom Filters

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## Abstract

There has been a recent trend in training neural networks to replace data structures that have been crafted by hand, with an aim for faster execution, better accuracy, or greater compression. In this setting, a neural data structure is instantiated by training a network over many epochs of its inputs until convergence. In applications where inputs arrive at high throughput, or are ephemeral, training a network from scratch is not practical. This motivates the need for few-shot neural data structures. In this paper we explore the learning of approximate set membership over a set of data in one-shot via meta-learning. We propose a novel memory architecture, the Neural Bloom Filter, which is able to achieve significant compression gains over classical Bloom Filters and existing memory-augmented neural networks.

## 1. Introduction

One of the simplest questions one can ask of a set of data is whether or not a given query is contained within it. Is  $q$ , our query, a member of  $S$ , our chosen set of observations? This *set membership* query arises across many computing domains; from databases, network routing, and firewalls. One could query set membership by storing  $S$  in its entirety and comparing  $q$  against each element. However, more space-efficient solutions exist.

The original and most widely implemented *approximate set membership* data-structure is the Bloom Filter (Bloom, 1970). It works by storing sparse distributed codes, produced from randomized hash functions, within a binary vector. The Bloom-filter trades off space for an allowed false positive rate, which arises due to hash collisions. However its error is one-sided; if an element  $q$  is contained in  $S$  then it will always be recognized. It never emits false nega-

tives. One can find Bloom Filters embedded within a wide range of production systems; from *network security* (Geravand & Ahmadi, 2013), to block malicious IP addresses; *databases*, such as Google’s Bigtable (Chang et al., 2008), to avoid unnecessary disk lookups; *cryptocurrency* (Hearn & Corallo, 2012), to allow clients to filter irrelevant transactions; *search*, such as Facebook’s typeahead search (Adams, 2010), to filter pages which do not contain query prefixes; and *program verification* (Dillinger & Manolios, 2004), to avoid recomputation over previously observed states.

While the main appeal of Bloom Filters is favourable compression, another important quality is the support for dynamic updates. New elements can be inserted in  $\mathcal{O}(1)$  time. This is not the case for all approximate set membership data structures. For example, perfect hashing saves  $\approx 40\%$  space over Bloom Filters but requires a pre-processing stage that is polynomial-time in the number of elements to store (Dietzfelbinger & Pagh, 2008). Whilst the static set membership problem is interesting, it limits the applicability of the algorithm. For example, in a database application that is serving a high throughput of write operations, it may be intractable to regenerate the full data-structure upon each batch of writes.

We thus focus on the data stream computation model (Muthukrishnan et al., 2005), where input observations are assumed to be ephemeral and can only be inspected a constant number of times — usually once. This captures many real-world applications: network traffic analysis, database query serving, and reinforcement learning in complex domains. Devising an approximate set membership data structure that is not only more compressive than Bloom Filters, but can be applied to either dynamic or static sets, could have a significant performance impact on modern computing applications. In this paper we investigate this problem using memory-augmented neural networks and meta-learning.

We build upon the recently growing literature on using neural networks to replace algorithms that are configured by heuristics, or do not take advantage of the data distribution. For example, Bloom Filters are indifferent to the data distribution. They have near-optimal space efficiency when data is drawn uniformly from a universe set (Carter et al., 1978) (maximal-entropy case) but (as we shall show) are sub-optimal when there is more structure. Prior studies on

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this theme have investigated compiler optimization (Cummins et al., 2017), computation graph placement (Mirhoseini et al., 2017), and data index structures such as b-trees (Kraska et al., 2018). In the latter work, Kraska et al. (2018) explicitly consider the problem of static set membership. By training a neural network over a fixed  $S$  (in their case, string inputs) along with held-out negative examples, they observe 36% space reduction over a conventional Bloom Filter<sup>1</sup>. Crucially this requires iterating over the storage set  $S$  a large number of times to embed its salient information into the weights of a neural network classifier. For a new  $S$  this process would have to be repeated from scratch.

Instead of learning from scratch, we draw inspiration from the few-shot learning advances obtained by meta-learning memory-augmented neural networks (Santoro et al., 2016; Vinyals et al., 2016). In this setup, tasks are sampled from a common distribution and a network learns to specialize to (learn) a given task with few examples. This matches very well to applications where many Bloom Filters are instantiated over different subsets of a common data distribution. For example, a Bigtable database usually contains one Bloom Filter per SSTable file. For a large table that contains Petabytes of data, say, there can be over 100,000 separate instantiated data-structures which share a common row-key format and query distribution. Meta-learning allows us to exploit this common redundancy. We design a database task with similar redundancy to investigate this exact application in Section 5.4.

The main contributions of this paper are (1) A new memory-augmented neural network architecture, the *Neural Bloom Filter*, which learns to write to memory using a distributed write scheme, and (2) An empirical evaluation of the Neural Bloom Filter meta-learned on one-shot approximate set membership problems of varying structure. We compare with the classical Bloom Filter alongside other memory-augmented neural networks such as the Differentiable Neural Computer (Graves et al., 2016) and Memory Networks (Sukhbaatar et al., 2015). We find when there is no structure, that differentiates the query set elements and queries, the Neural Bloom Filter learns a solution similar to a Bloom Filter derivative — a Bloom-g filter (Qiao et al., 2011) — but when there is a lot of structure the solution can be considerably more compressive (e.g. 30× for a database task).

## 2. Background

### 2.1. Approximate Set Membership

The problem of *exact set membership* is to state whether or not a given query  $q$  belongs to a set of  $n$  distinct observa-

<sup>1</sup>The space saving increases to 41% when an additional trick is incorporated, in discretizing and re-scaling the classifier outputs and treating the resulting function as a hash function to a bit-map.

tions  $S = \{x_1, \dots, x_n\}$  where  $x_i$  are drawn from a universe set  $U$ . By counting the number of distinct subsets of size  $n$  it can be shown that any such exact set membership tester requires at least  $\log_2 \binom{|U|}{n}$  bits of space. To mitigate the space dependency on  $|U|$ , which can be prohibitively large, one can relax the constraint on perfect correctness. *Approximate set membership* allows for a false positive rate of at most  $\epsilon$ . Specifically we answer  $q \in A(S)$  where  $A(S) \supseteq S$  and  $p(q \in A(S) - S) \leq \epsilon$ . It can be shown<sup>2</sup> the space requirement for approximate set membership of uniformly sampled observations is at least  $n \log_2(\frac{1}{\epsilon})$  bits (Carter et al., 1978) which can be achieved with perfect hashing. So for a false positive rate of 1%, say, this amounts to 6.6 bits per element. In contrast to storing raw or compressed elements this can be a huge space saving, for example ImageNet images require 108 KB per image on average when compressed with JPEG, an increase of over four orders of magnitude.

### 2.2. Bloom Filter

The Bloom Filter (Bloom, 1970) is a data structure which solves the dynamic approximate set membership problem with near-optimal space complexity. It assumes access to  $k$  uniform hash functions  $h_i : U \rightarrow \{1, \dots, m\}$ ,  $i = 1, \dots, k$  such that  $p(h_i(x) = j) = 1/m$  independent of prior hash values or input  $x$ . The Bloom Filter’s memory  $M \in [0, 1]^m$  is a binary string of length  $m$  which is initialized to zero. Writes are performed by hashing an input  $x$  to  $k$  locations in  $M$  and setting the corresponding bits to 1,  $M[h_i(x)] \leftarrow 1$ ;  $i = 1, \dots, k$ . For a given query  $q$  the Bloom Filter returns true if all corresponding hashed locations are set to 1 and returns false otherwise:  $Query(M, q) := M[h_1(q)] \wedge M[h_2(q)] \wedge \dots \wedge M[h_k(q)]$ . This incurs zero false negatives, as any previously observed input must have enabled the corresponding bits in  $M$ , however there can be false positives due to hash collisions. To achieve a false positive rate of  $\epsilon$  with minimal space one can set  $k = \log_2(1/\epsilon)$  and  $m = n \log_2(1/\epsilon) \log_2 e$ , where  $e$  is Euler’s number. The resulting space is a factor of  $\log_2 e \approx 1.44$  from the optimal static lower bound given by Carter et al. (1978).

### 2.3. Memory-Augmented Neural Networks

Recurrent neural networks such as LSTMs retain a small amount of memory via the recurrent state. However this is usually tied to the number of trainable parameters in the model. There has been recent interest in augmenting neural networks with a larger external memory. The method for doing so, via a differentiable write and read interface, was first popularized by the Neural Turing Machine (NTM) (Graves et al., 2014) and its successor the Differentiable Neural

<sup>2</sup>By counting the minimal number of  $A(S)$  sets required to cover all  $S \subset U$ .

Computer (DNC) (Graves et al., 2016) in the context of learning algorithms, and by Memory Networks (Sukhbaatar et al., 2015) in the context of question answering. Memory Networks store embeddings of the input in separate rows of a memory matrix  $M$ . Reads are performed via a differentiable *content-based addressing* operation. Given a query embedding  $q$  we take some similarity measure  $D$  (e.g. cosine similarity, or negative euclidean distance) against each row in memory and apply a softmax to obtain a *soft* address vector  $a \propto e^{D(q,M)}$ . A read is then a weighted sum over memory  $r \leftarrow a^T M$ . The NTM and DNC use the same content-based read mechanism, but also learns to write. These models can arbitrate whether to write to slots in memory with similar content (content-based writes), temporally ordered locations, or unused memory.

When it comes to capacity, there has been consideration to scaling both the DNC and Memory Networks to very large sizes using sparse read and write operations (Rae et al., 2016; Chandar et al., 2016). However another way to increase the capacity is to increase the amount of compression which occurs in memory. Memory Nets can create compressive representations of each input, but cannot compress jointly over multiple inputs because they are hard-wired to write one slot per timestep. The NTM and DNC can compress over multiple slots in memory because they can arbitrate writes across multiple locations, but in practice seem to choose very sharp read and write addresses. The Kanerva Machine (Wu et al., 2018a;b) tackles memory-wide compression using a distributed write scheme to jointly compose and compress its memory contents. The model uses content-based addressing over a separate learnable addressing matrix  $A$ , instead of the memory  $M$ , and thus learns *where* to write. We take inspiration from this scheme.

### 3. Model

One approach to learning set membership in one-shot would be to use a recurrent neural network, such as an LSTM or DNC. Here, the model sequentially ingests the  $N$  elements to store, answers a set of queries using the final state, and is trained by BPTT. Whilst this is a general training approach, and the model may learn a compressive solution, it does not scale well to larger number of elements. Even when  $N = 1000$ , backpropagating over a sequence of this length induces computational and optimization challenges. For larger values this quickly becomes intractable. Alternatively one could store an embedding of each element  $x_i \in S$  in a slot-based Memory Network. This is more scalable as it avoids BPTT, because the gradients of each input can be calculated in parallel. However Memory Networks are not a space efficient solution (as shown in in Section 5) because there is no joint compression of inputs.

This motivates the proposed memory model, the Neural

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#### Algorithm 1 Neural Bloom Filter

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1: def controller(x):
2:    $z \leftarrow f_{enc}(x)$  // Input embedding
3:    $q \leftarrow f_q(z)$  // Query word
4:    $a \leftarrow \sigma(q^T A)$  // Memory address
5:    $w \leftarrow f_w(z)$  // Write word

6: def write(x):
7:    $a, w \leftarrow controller(x)$ 
8:    $M_{t+1} \leftarrow M_t + wa^T$  // Additive write

9: def read(x):
10:   $a, w, z \leftarrow controller(x)$ 
11:   $r \leftarrow flatten(M \odot a)$  // Read words
12:   $o \leftarrow f_{out}([r, w, z])$  // Output logit

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Bloom Filter. Briefly, the network is augmented with a real-valued memory matrix. The network *addresses* memory by classifying which memory slots to read or write to via a softmax, conditioned on the input. We can think of this as a continuous analogue to the Bloom Filter’s hash function; because it is learned the network can co-locate or separate inputs to improve performance. The network updates memory with a simple *additive write* operation — i.e. no multiplicative gating or squashing — to the addressed locations. An additive write operation can be seen as a continuous analogue to the the Bloom Filter’s logical OR write operation. Crucially, the additive write scheme allows us to train the model without BPTT — this is because gradients with respect to the write words  $\partial L / \partial w = (\partial L / \partial M)^T a$  can be computed in parallel. Reads involve a component-wise multiplication of address and memory (analogous to the selection of locations in the Bloom Filter via hashing), but instead of projecting this down to a scalar with a fixed function, we pass this through an MLP to obtain a scalar familiarity logit. The network is fully differentiable, allows for memories to be stored in a distributed fashion across slots, and is quite simple e.g. in comparison to DNCs.

The full architecture depicted in Figure 1 consists of a *controller network* which encodes the input to an embedding  $z \leftarrow f_{enc}(x)$  and transforms this to a write word  $w \leftarrow f_w(z)$  and a query  $q \leftarrow f_q(z)$ . The address over memory is computed via a softmax  $a \leftarrow \sigma(q^T A)$  over the content-based attention between  $q$  and a learnable address matrix  $A$ . Here,  $\sigma$  denotes a softmax. The network thus learns where to place elements or overlap elements based on their content, we can think of this as a soft and differentiable relaxation of the uniform hashing families incorporated by the Bloom Filter (see Appendix A.3 for further discussion).

A *write* is performed by running the controller to obtain a write word  $w$  and address  $a$ , and then additively writing  $w$  to  $M$ , weighted by the address  $a$ ,  $M_{t+1} \leftarrow M_t + wa^T$ . The

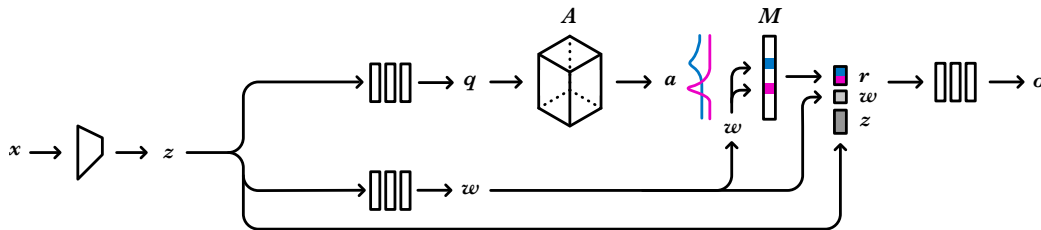


Figure 1. Overview of the Neural Bloom Filter architecture.

simple additive write ensures that the resulting memory is invariant to input ordering (as addition is commutative) and we do not have to backpropagate-through-time (BPTT) over sequential writes — gradients can be computed in parallel. A *read* is performed by also running the controller network to obtain  $z, w$ , and  $a$  and component-wise multiplying the address  $a$  with  $M$ ,  $r \leftarrow M \odot a$ . The read words  $r$  are fed through an MLP along with the residual inputs  $w$  and  $z$  and are projected to a single scalar logit, indicating the familiarity signal. We found this to be more powerful than the conventional read operation  $r \leftarrow a^T M$  used by the DNC and Memory Networks, as it allows for non-linear interactions between rows in memory at the time of read. See Algorithm 1 for an overview of the operations.

To give an example network configuration, we chose  $f_{enc}$  to be a 3-layer CNN in the case of image inputs, and a 128-hidden-unit LSTM in the case of text inputs. We chose  $f_w$  and  $f_q$  to be an MLP with a single hidden layer of size 128, followed by layer normalization, and  $f_{out}$  to be a 3-layer MLP with residual connections. We used a leaky ReLU as the non-linearity. Although the described model uses dense operations that scale linearly with the memory size  $m$ , we discuss how the model could be implemented for  $\mathcal{O}(\log m)$  time reads and writes using sparse attention and read/write operations, in Appendix A.1. Furthermore the model’s relation to uniform hashing is discussed in Appendix A.3.

## 4. Space Complexity

In this section we discuss space lower bounds for the approximate set membership problem when there is some structure to the storage or query set. This can help us formalise why and where neural networks may be able to beat classical lower bounds to this problem.

The  $n \log_2(1/\epsilon)$  lower bound from Carter et al. (1978) assumes that all subsets  $S \subset U$  of size  $n$ , and all queries  $q \in U$  have equal probability. Whilst it is instructive to bound this maximum-entropy scenario, which we can think of as ‘worst case’, most applications of approximate set membership e.g. web cache sharing, querying databases, or spell-checking, involve sets and queries that are not sampled uniformly. For example, the elements within a given set may

be highly dependent, there may be a power-law distribution over queries, or the queries and sets themselves may not be sampled independently.

A more general space lower bound can be defined by an information theoretic argument from communication complexity (Yao, 1979). Namely, approximate set membership can be framed as a two-party communication problem between Alice, who observes the set  $S$  and Bob, who observes a query  $q$ . They can agree on a shared policy  $\Pi$  in which to communicate. For given inputs  $S, q$  they can produce a transcript  $A_{S,q} = \Pi(S, q) \in \mathcal{Z}$  which can be processed  $g : \mathcal{Z} \rightarrow 0, 1$  such that  $\mathbb{P}(g(A_{S,q}) = 1 | q \notin S) \leq \epsilon$ . Bar-Yossef et al. (2004) shows that the maximum transcript size is greater than the mutual information between the inputs and transcript:  $\max_{S,q} |A_{S,q}| \geq I(S, q; A_{S,q}) = H(S, q) - H(S, q | A_{S,q})$ . Thus we note problems where we may be able to use less space than the classical lower bound are cases where the entropy  $H(S, q)$  is small, e.g. our sets are highly non-uniform, or cases where  $H(S, q | A_{S,q})$  is large, which signifies that many query and set pairs can be solved with the same transcript.

## 5. Experiments

Our experiments explore scenarios where set membership can be learned in one-shot with improved compression over the classical Bloom Filter. We consider tasks with varying levels of structure in the storage sets  $S$  and queries  $q$ . We compare the Neural Bloom Filter with three memory-augmented neural networks, the LSTM, DNC, and Memory Network, that are all able to write storage sets in one-shot.

The training setup follows the memory-augmented meta-learning training scheme of Vinyals et al. (2016), only here the task is familiarity classification versus image classification. The network samples tasks which involve classifying familiarity for a given storage set. Meta-learning occurs as a two-speed process, where the model quickly learns to recognize a given storage set  $S$  within a training episode via writing to a memory or state, and the model slowly learns to improve this fast-learning process by optimizing the model parameters  $\theta$  over multiple tasks. We detail the training routine in Algorithm 2.

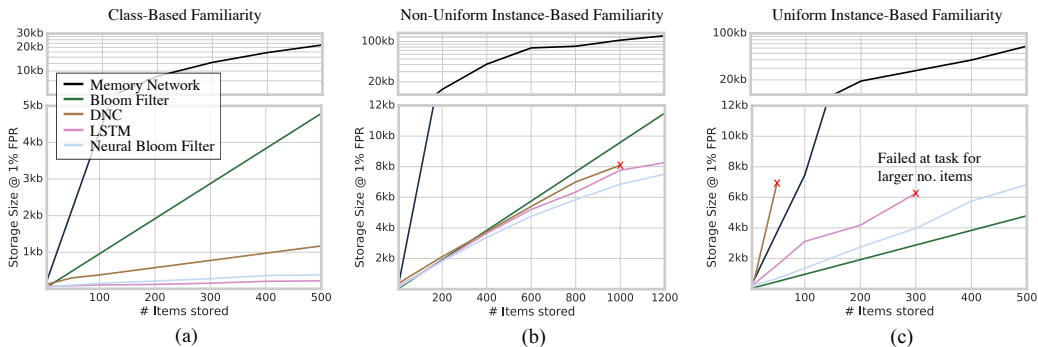


Figure 2. Sampling strategies on MNIST. Space consumption at 1% FPR.

**Algorithm 2** Meta-Learning Training

- 1: Let  $S^{train}$  denote the distribution over sets to store.
- 2: Let  $Q^{train}$  denote the distribution over queries.
- 3: **for**  $i = 1$  **to** max train steps **do**
- 4:   Sample task:
- 5:     Sample set to store:  $S \sim S^{train}$
- 6:     Sample  $t$  queries:  $x_1, \dots, x_t \sim Q^{train}$
- 7:     Targets:  $y_j = 1$  if  $x_j \in S$  else 0;  $j = 1, \dots, t$
- 8:     Write entries to memory:  $M \leftarrow f_{\theta}^{write}(S)$
- 9:     Calculate logits:  $o_j = f_{\theta}^{read}(M, x_j)$ ;  $j = 1, \dots, t$
- 10:    XE loss:  $L = \sum_{j=1}^t y_j \log o_j + (1 - y_j)(1 - \log o_j)$
- 11:    Backprop through queries and writes:  $dL/d\theta$
- 12:    Update parameters:  $\theta_{i+1} \leftarrow \text{Optimizer}(\theta_i, dL/d\theta)$
- 13: **end for**

For the RNN baselines (LSTM and DNC) the write operation corresponds to unrolling the network over the inputs and outputting the final state. For these models, the query network is simply an MLP classifier which receives the concatenated final state and query, and outputs a scalar logit. For the Memory Network, inputs are stored in individual slots and the familiarity signal is computed from the maximum content-based attention value. The Neural Bloom Filter read and write operations are defined in Algorithm 1.

**5.1. Space Comparison**

We compared the space (in bits) of the model’s memory (or state) to a Bloom Filter at a given false positive rate and 0% false negative rate. The false positive rate is measured empirically over a sample of 50,000 queries for the learned models; for the Bloom Filter we employ the analytical false positive rate. Beating a Bloom Filter’s space usage with the analytical false positive rate implies better performance for any given Bloom Filter library version (as actual Bloom Filter hash functions are not uniform), thus the comparison is reasonable. For each model we sweep over hyper-parameters relating to model size to obtain their

smallest operating size at the desired false positive rate (for the full set, see Appendix D). Because the neural models can emit false negatives, we store these in a (ideally small) backup Bloom Filter, as proposed by Kraska et al. (2018); Mitzenmacher (2018a). We account for the space of this backup Bloom Filter, and add it to the space usage of the model’s memory for parity (See Appendix B for further discussion). The neural network must learn to output a small state in one-shot that can serve set membership queries at a given false positive rate, and emit a small enough number of false negatives such that the backup filter is also small, and the total size is considerably less than a Bloom Filter.

**5.2. Sampling Strategies on MNIST**

To understand what kinds of scenarios neural networks may be more (or less) compressive than classical Bloom Filters, we consider three simple set membership tasks that have a graded level of structure to the storage sets and queries. Concretely, they differ in the sampling distribution of storage sets  $S^{train}$  and queries  $Q^{train}$ . However all problems are approximate set membership tasks that can be solved by a Bloom Filter. The tasks are (1) *Class-based familiarity*, a highly structured task where each set of images is sampled with the constraint that they arise from the same randomly-selected class. (2) *Non-uniform instance-based familiarity*, a moderately structured task where the images are sampled without replacement from an exponential distribution. (3) *Uniform instance-based familiarity*, a completely unstructured task where each subset contains images sampled uniformly without replacement. For each task we varied the size of the sample set to store, and calculated the space (in bits) of each model’s state at a fixed false positive rate of 1% and a false negative rate of 0%. We used relatively small storage set sizes (e.g. 100 – 1000) to start with, as this highlights that some RNN-based approaches struggle to train over larger set sizes, before progressing to larger sets in subsequent sections. See Appendix E for further details on the task setup. In the *class-based sampling* task we see in Figure 2a that the DNC, LSTM and Neural Bloom Filter are

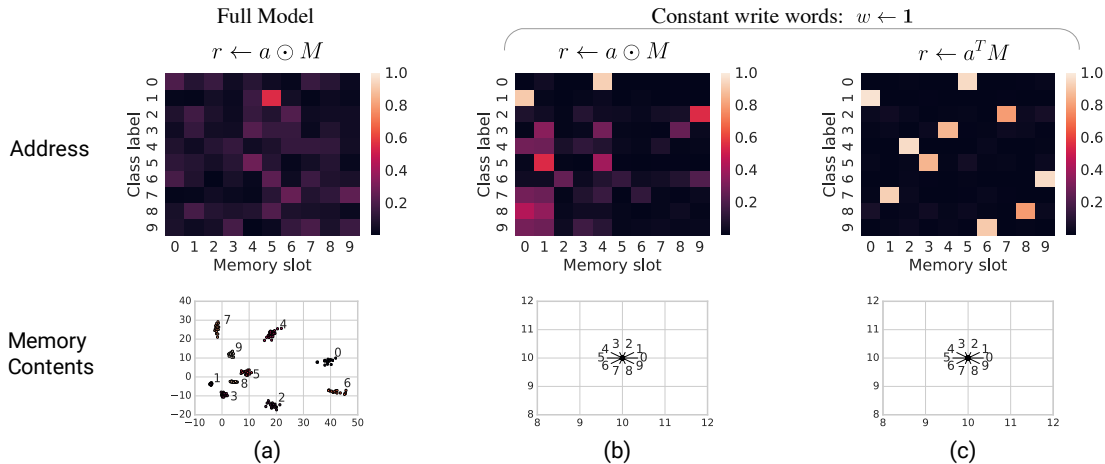


Figure 3. **Memory access analysis.** Three different learned solutions to class-based familiarity. We train three Neural Bloom Filter variants, with a succession of simplified read and write mechanisms. Each model contains 10 memory slots and the memory addressing weights  $a$  and contents  $\bar{M}$  are visualised, broken down by class. Solutions share broad correspondence to known algorithms: (a) Bloom-g filters, (b) Bloom Filters, (c) Perfect hashing.

able to significantly outperform the classical Bloom Filter when images are sampled by class. The Memory Network is able to solve the task with a word size of only 2, however this corresponds to a far greater number of bits per element, 64 versus the Bloom Filter’s 9.8 (to a total size of 4.8kb), and so the overall size was prohibitive. The DNC, LSTM, and Neural Bloom Filter are able to solve the task with a storage set size of 500 at 1.1kb, 217b, and 382b; a 4.3×, 22×, and 12× saving respectively. For the *non-uniform sampling task* in Figure 2b we see the Bloom Filter is preferable for less than 500 stored elements, but is overtaken thereafter. At 1000 elements the DNC, LSTM, and Neural Bloom Filter consume 7.9kb, 7.7kb, and 6.8kb respectively which corresponds to a 17.6%, 19.7%, and 28.6% reduction over the 9.6kb Bloom Filter. In the *uniform sampling task* shown in Figure 2c, there is no structure to the sampling of  $S$ . The two architectures which rely on BPTT essentially fail to solve the task at some threshold of storage size. The Neural Bloom Filter solves it with 6.8kb (using a memory size of 50 and word size of 2). The overall conclusion from these sets of experiments is that the classical Bloom Filter works best when there is no structure to the data, however when there is (e.g. skewed data, or highly dependent sets that share common attributes) we do see significant space savings.

### 5.3. Memory Access Analysis

We wanted to understand how the Neural Bloom Filter uses its memory, and in particular how its learned solutions may correspond to classical algorithms. We inspected the memory contents (what was stored to memory) and addressing weights (where it was stored) for a small model of 10 mem-

ory slots and a word size of 2, trained on the MNIST class-based familiarity task. We plot this for each class label, and compare the pattern of memory usage to two other models that use increasingly simpler read and write operations: (1) an ablated model with constant write words  $w \leftarrow \mathbf{1}$ , and (2) an ablated model with  $w \leftarrow \mathbf{1}$  and a linear read operator  $r \leftarrow a^T M$ .

The full model, shown in Figure 3a learns to place some classes in particular slots, e.g. class 1  $\rightarrow$  slot 5, however most are distributed. Inspecting the memory contents, it is clear the write word encodes a unique 2D token for each class. This solution bears resemblance with Bloom-g Filters (Qiao et al., 2011) where elements are spread across a smaller memory with the same hashing scheme as Bloom Filters, but a unique token is stored in each slot instead of a constant 1-bit value. With the model ablated to store only 1s in Figure 3b we see it uses semantic addressing codes for some classes (e.g. 0 and 1) and distributed addresses for other classes. E.g. for class 3 the model prefers to uniformly spread its writes across memory slot 1, 4, and 8. The model solution is similar to that of Bloom Filters, with distributed addressing codes as a solution — but no information in the written words themselves. When we force the read operation to be linear in Figure 3c, the network maps each input class to a unique slot in memory. This solution has a correspondence with perfect hashing. In conclusion, with small changes to the read/write operations we see the Neural Bloom Filter learn different algorithmic solutions.

### 5.4. Database Queries

We look at a task inspired by database interactions. NoSQL databases, such as Bigtable and Cassandra, use a single string-valued row-key, which is used to index the data. The

	5%	1%	0.1%
Neural Bloom Filter	871b	1.5kb	24.5kb
Bloom Filter	31.2kb	47.9kb	72.2kb
Cuckoo Filter	33.1kb	45.3kb	62.6kb

Table 1. **Database task.** Storing 5000 row-key strings for a target false positive rate.

database is comprised of a union of files (e.g. SSTables) storing contiguous row-key chunks. Bloom Filters are used to determine whether a given query  $q$  lies within the stored set. We emulate this setup by constructing a universe of strings, that is alphabetically ordered, and by sampling contiguous ranges (to represent a given SSTable). Queries are sampled uniformly from the universe set of strings. We choose the 2.5M unique tokens in the GigaWord v5 news corpus to be our universe as this consists of structured natural data and some noisy or irregular strings.

We consider the task of storing sorted string sets of size 5000. We train the Neural Bloom Filter to several desired false positive rates (5%, 1%, 0.1%) and used a backup Bloom Filter to guarantee 0% false negative rate. We also trained LSTMs and DNCs for comparison, but they failed to learn a solution to the task after several days of training; optimizing insertions via BPTT over a sequence of length 5000 did not result in a remotely usable solution. The Neural Bloom Filter avoids BPTT via its simple additive write scheme, and so it learned to solve the task quite naturally. As such, we compare the Neural Bloom Filter solely to classical data structures: Bloom Filters and Cuckoo Filters. In Table 1 we see a significant space reduction of 3 – 40 $\times$ , where the margin grows with increasing permitted false positive rates. Since memory is an expensive component within production databases (in contrast to disk, say), this memory space saving could translate to a non-trivial cost reduction. We note that a storage size of 5000 may appear small, but is relevant to the NOSQL database scenario where disk files (e.g. SSTables) are typically sharded to be several megabytes in size, to avoid issues with compaction. E.g. if the stored values were of size 10kB per row, we would expect 5000 unique keys or less in an average Bigtable SSTable.

One further consideration for production deployment is the ability to extrapolate to larger storage set sizes during evaluation. We investigate this for the Neural Bloom Filter on the same database task, and compare it to an LSTM. To ensure both models train, we set the maximum training storage set size to 200 and evaluate up to sizes 250, a modest 25% size increase. We find that the Neural Bloom Filter uses up to 3 $\times$  less space than the LSTM and the neural models are able to extrapolate to larger set sizes than those observed during training (see Appendix F Figure 4). Whilst the performance eventually degrades when the training limit size is exceeded,

it is not catastrophic for either the LSTM or Neural Bloom Filter.

## 5.5. Timing benchmark

We have principally focused on space comparisons in this paper, we now consider speed for the database task described in the prior section. We measure latency as the wall-clock time to complete a single insertion or query of a row-key string of length 64. We also measure throughput as the reciprocal wall-clock time of inserting or querying 10,000 strings. We use a common encoder architecture for the neural models, a 128-hidden-unit character LSTM. We benchmark the models on the CPU (Intel(R) Xeon(R) CPU E5-1650 v2 @ 3.50GHz) and on the GPU (NVIDIA Quadro P6000) with models implemented in TensorFlow without any model-specific optimizations. We compare to empirical timing results published in a query-optimized Bloom Filter variant (Chen et al., 2007). We include the Learned Index from (Kraska et al., 2018) to contrast timings with a model that is not one-shot. The architecture is simply the LSTM character encoder; inserts are performed via gradient descent. The number of gradient-descent steps to obtain convergence is domain-dependent, we chose 50 steps in our timing benchmarks. The Learned Index queries are obtained by running the character LSTM over the input and classifying familiarity — and thus query metrics are identical to the LSTM baseline.

We see in Table 2. that the combined query and insert latency of the Neural Bloom Filter and LSTM sits at 5ms on the CPU, around 400 $\times$  slower than the classical Bloom Filter. The Learned Index contains a much larger latency of 780ms due to the sequential application of gradients. For all neural models, latency is not improved when operations are run on the GPU. However when multiple queries are received, the throughput of GPU-based neural models surpasses the classical Bloom Filter due to efficient concurrency of the dense linear algebra operations. This leads to the conclusion that a Neural Bloom Filter could be deployed in scenarios with high query load without a catastrophic decrease in throughput, if GPU devices are available. For insertions we see a bigger separation between the one-shot models: the LSTM and Neural Bloom Filter. Whilst all neural models are uncompetitive on the CPU, the Neural Bloom Filter surpasses the Bloom Filter’s insertion throughput when placed on the GPU, with 101K insertions per second (IPS). The LSTM runs at 4.6K IPS, one order of magnitude slower, because writes are serial, and the Learned Index structure is two orders of magnitude slower at 816 IPS due to sequential gradient computations. The benefits of the Neural Bloom Filter’s simple write scheme are apparent here.

## Meta-Learning Neural Bloom Filters

	Query + Insert Latency		Query Throughput (QPS)		Insert Throughput (IPS)	
	CPU	GPU	CPU	GPU	CPU	GPU
Bloom Filter*	<b>0.02ms</b>	-	61K	-	61K	-
Neural Bloom Filter	5.1ms	13ms	3.5K	105K	3.2K	<b>101K</b>
LSTM	5.0ms	13ms	3.1K	<b>107K</b>	2.4K	4.6K
Learned Index (Kraska et al., 2018)	780ms	1.36s	3.1K	<b>107K</b>	25	816

Table 2. Latency for a single query, and throughput for a batch of 10,000 queries. \*Query-efficient Bloom Filter from Chen et al. (2007).

## 6. Related Work

There have been a large number of Bloom Filter variants published; from *Counting Bloom Filters* which support deletions (Fan et al., 2000), *Bloomier Filters* which store functions vs sets (Chazelle et al., 2004), *Compressed Bloom Filters* which use arithmetic encoding to compress the storage set (Mitzenmacher, 2002), and *Cuckoo Filters* which use cuckoo hashing to reduce redundancy within the storage vector (Fan et al., 2014). Although some of these variants focus on better compression, they do not achieve this by specializing to the data distribution.

One of the few works which address data-dependence are *Weighted Bloom Filters* (Bruck et al., 2006; Wang et al., 2015). They work by modulating the number of hash functions used to store or query each input, dependent on its storage and query frequency. This requires estimating a large number of separate storage and query frequencies. This approach can be useful for imbalanced data distributions, such as the non-uniform instance-based MNIST familiarity task. However it cannot take advantage of dependent sets, such as the class-based MNIST familiarity task, or the database query task. We see the Neural Bloom Filter is more compressive in all settings.

Sterne (2012) proposes a neurally-inspired set membership data-structure that works by replacing the randomized hash functions with a randomly-wired computation graph of *OR* and *AND* gates. The false positive rate is controlled analytically by modulating the number of gates and the overall memory size. However there is no learning or specialization to the data with this setup. Bogacz & Brown (2003) investigates a learnable neural familiarity module, which serves as a biologically plausible model of familiarity mechanisms in the brain, namely within the perirhinal cortex. However this has not shown to be empirically effective at exact matching.

Kraska et al. (2018) consider the use of a neural network to classify the membership of queries to a fixed set  $S$ . Here the network itself is more akin to a perfect hashing setup where multiple epochs are required to find a succinct holistic representation of the set, which is embedded into the weights of the network. In their case this search is performed by gradient-based optimization. We emulate their experimental comparison approach but instead propose a

memory architecture that represents the set as activations in memory, versus weights in a network.

Mitzenmacher (2018a) discusses the benefits and drawbacks of a learned Bloom Filter; distinguishing the empirical false positive rate over the distribution of sets  $S$  versus the conditional false positive rate of the model given a particular set  $S$ . In this paper we focus on the empirical false positive rate because we wish to exploit redundancy in the data and query distribution. Mitzenmacher (2018b) also considers an alternate way to combine classical and learned Bloom Filters by ‘sandwiching’ the learned model with pre-filter and post-filter classical Bloom Filters to further reduce space.

## 7. Conclusion

In many situations neural networks are not a suitable replacement to Bloom Filters and their variants. The Bloom Filter is robust to changes in data distribution because it delivers a bounded false positive rate for any sampled subset. However in this paper we consider the questions, “When might a single-shot neural network provide better compression than a Bloom Filter?”. We see that a model which uses an external memory with an adaptable capacity, avoids BPTT with a feed-forward write scheme, and learns to address its memory, is the most promising option in contrast to popular memory models such as DNCs and LSTMs. We term this model the Neural Bloom Filter due to the analogous incorporation of a hashing scheme, commutative write scheme, and multiplicative read mechanism.

The Neural Bloom Filter relies on settings where we have an off-line dataset (both of stored elements and queries) that we can meta-learn over. In the case of a large database we think this is warranted, a database with 100K separate set membership data structures will benefit from a single (or periodic) meta-learning training routine that can run on a single machine and sample from the currently stored data, generating a large number of efficient data-structures. We envisage the space cost of the network to be amortized by sharing it across many neural Bloom Filters, and the time-cost of executing the network to be offset by the continuous acceleration of dense linear algebra on modern hardware, and the ability to batch writes and queries efficiently. A promising future direction would be to investigate the feasibility of this approach in a production system.



## Acknowledgments

We thank Peter Dayan, Yori Zwols, Yan Wu, Joel Leibo, Greg Wayne, Andras Gyorgy, Charles Blundell, Daan Weirstra, Pushmeet Kohli, and Tor Lattimor for their insights during this project.

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