# Near Optimal Methods for Minimizing Convex Functions with Lipschitz *p*-th Derivatives

Alexander Gasnikov Moscow Institute of Physics and Technology, Institute for search University Higher School of Economics	GASNIKOV@YANDEX.RU or Information Transmission Problems, National Re-
<b>Pavel Dvurechensky</b> Weierstrass Institute for Applied Analysis and Stochastic	PAVEL.DVURECHENSKY@GMAIL.COM cs, Institute for Information Transmission Problems
<b>Eduard Gorbunov</b> Moscow Institute of Physics and Technology	EDUARD.GORBUNOV@PHYSTECH.EDU
<b>Evgeniya Vorontsova</b> Grenoble Alpes University & Far Eastern Federal Unive	VORONTSOVAEA@GMAIL.COM ersity, Russia
<b>Daniil Selikhanovych</b> Moscow Institute of Physics and Technology, Institute fo	SELIHANOVICH.DO@PHYSTECH.EDU or Information Transmission Problems
<b>César A. Uribe</b> Massachusetts Institute of Technology	CAURIBE@MIT.EDU
<b>Bo Jiang</b> Shanghai University of Finance and Economics	ISYEBOJIANG@GMAIL.COM
<b>Haoyue Wang</b> Fudan University	HAOYUEWANG14@FUDAN.EDU.CN
<b>Shuzhong Zhang</b> University of Minnesota & The Chinese University of He	ZHANGS@UMN.EDU ong Kong, Shenzhen
<b>Sébastien Bubeck</b> Microsoft Research	SEBUBECK@MICROSOFT.COM
<b>Qijia Jiang</b> Stanford University	QJIANG2@STANFORD.EDU
<b>Yin Tat Lee</b> University of Washington & Microsoft Research	YINTAT@UW.EDU
<b>Yuanzhi Li</b> Stanford University	YUANZHIL@STANFORD.EDU
Aaron Sidford	SIDFORD@STANFORD.EDU

Editors: Alina Beygelzimer and Daniel Hsu

Stanford University

## Abstract

In this merged paper, we consider the problem of minimizing a convex function with Lipschitzcontinuous *p*-th order derivatives. Given an oracle which when queried at a point returns the first *p*-derivatives of the function at that point we provide some methods which compute an  $\varepsilon$  approximate minimizer in  $O\left(\varepsilon^{-\frac{2}{3p+1}}\right)$  iterations. These methods match known lower bounds up to polylogarithmic factors for constant *p*.

# 1. Results

See Gasnikov et al. (2018); Jiang et al. (2018); Bubeck et al. (2018) for details.

#### Acknowledgments

The authors are grateful to Yurii Nesterov for fruitful discussions. The work of A. Gasnikov was supported by RFBR 18-29-03071 mk and was prepared within the framework of the HSE University Basic Research Program and funded by the Russian Academic Excellence Project '5-100'. The work of P. Dvurechensky and E. Vorontsova was supported by RFBR 18-31-20005 mol-a-ved. The work of E. Gorbunov was supported by the grant of Russian's President MD-1320.2018.1. The work of Bo Jiang was supported by NSFC grant 11771269. The work of Yin Tat Lee was supported by NSF Awards CCF-1740551, CCF-1749609, and DMS-1839116. The work of Aaron Sidford was supported by NSF CAREER Award CCF-1844855.

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