

Contrastive Example-Based Control

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Abstract

While many real-world problems that might benefit from reinforcement learning, these problems rarely fit into the MDP mold: interacting with the environment is often expensive and specifying reward functions is challenging. Motivated by these challenges, prior work has developed data-driven approaches that learn entirely from samples from the transition dynamics and examples of high-return states. These methods typically learn a reward function from high-return states, use that reward function to label the transitions, and then apply an offline RL algorithm to these transitions. While these methods can achieve good results on many tasks, they can be complex, often requiring regularization and temporal difference updates. In this paper, we propose a method for offline, example-based control that learns an implicit model of multi-step transitions, rather than a reward function. We show that this implicit model can represent the Q-values for the example-based control problem. Across a range of state-based and image-based offline control tasks, our method outperforms baselines that use learned reward functions; additional experiments demonstrate improved robustness and scaling with dataset size.

Keywords: reinforcement learning, offline RL, robot learning, reward learning, contrastive learning, model-based reinforcement learning, example-based control, reward-free learning

1. Introduction

Reinforcement learning is typically framed as the problem of maximizing a given reward function. However, in many real-world situations, it is more natural for users to define what they want an agent to do with examples of successful outcomes (Fu et al., 2018b; Zolna et al., 2020a; Xu and Denil, 2019; Eysenbach et al., 2021). For example, a user that wants their robot to pack laundry into a washing machine might provide multiple examples of states where the laundry has been packed correctly. This problem setting is often seen as a variant of inverse reinforcement learning (Fu et al., 2018b), where the aim is to learn only from examples of successful outcomes, rather than from expert demonstrations. To solve this problem, the agent must both figure out what constitutes task success (i.e., what the examples have in common) and how to achieve such successful outcomes.

In this paper, our aim is to address this problem setting in the case where the agent must learn from offline data without trial and error. Instead, the agent must infer the outcomes of potential actions from the provided data, while also relating these inferred outcomes to the success examples. We will refer to this problem of offline RL with success examples as *offline example-based control*.

Most prior approaches involve two steps: *first* learning a reward function, and *second* combining it with an RL method to recover a policy (Fu et al., 2018b; Zolna et al., 2020a; Xu and Denil, 2019). While such approaches can achieve excellent results when provided sufficient data (Kalashnikov et al., 2021; Zolna et al., 2020a), learning the reward function is challenging when the number of success examples is small (Li et al., 2021; Zolna et al., 2020a). Moreover, these prior approaches are relatively complex (e.g., they use temporal difference learning) and have many hyperparameters.

Our aim is to provide a simple and scalable approach that avoids the challenges of reward learning. The main idea will be learning a certain type of dynamics model. Then, using that model to predict the probabilities of reaching each of the success examples, we will be able to estimate the Q-values for every state and action. Note that this approach does not use an offline RL algorithm as a subroutine. The key design decision is the model type; we will use an implicit model of the time-averaged future (precisely, the discounted state occupancy measure). This decision means that our model reasons across multiple time steps but will not output high-dimensional observations (only a scalar number). A limitation of this approach is that it will correspond to a single step of policy improvement: the dynamics model corresponds to the dynamics of the behavioral policy, not of the reward-maximizing policy. While this means that our method is not guaranteed to yield the optimal policy, our experiments nevertheless show that our approach outperforms multi-step RL methods.

The main contribution of this paper is an offline RL method (LAEO) that learns a policy from examples of high-reward states. The key idea behind LAEO is an implicit dynamics model, which represents the probability of reaching states at some point in the future. We use this model to estimate the probability of reaching examples of high-return states. LAEO is simpler yet more effective than prior approaches based on reward classifiers. Our experiments demonstrate that LAEO can successfully solve offline RL problems from examples of high-return states on four state-based and two image-based manipulation tasks. Our experiments show that LAEO is more robust to occlusions and also exhibits better scaling with dataset size than prior methods. We also show that LAEO can work in example-based control settings in which goal-conditioned RL methods fail.

2. Related Work

Reward learning. To overcome the challenge of hand-engineering reward functions for RL, prior methods either use supervised learning or adversarial training to learn a policy that matches the expert behavior given by the demonstration (imitation learning) (Pomerleau, 1988; Ross et al., 2011; Ho and Ermon, 2016; Spencer et al., 2021) or learn a reward function from demonstrations and optimize the policy with the learned reward through trial and error (inverse RL) (Ng and Russell, 2000; Abbeel and Ng, 2004; Ratliff et al., 2006; Ziebart et al., 2008; Finn et al., 2016; Fu et al., 2018a). However, providing full demonstrations complete with agent actions is often difficult, therefore, recent works have focused on the setting where only a set of user-specified goal states or human videos are available (Fu et al., 2018b; Singh et al., 2019; Kalashnikov et al., 2021; Xie et al., 2018; Eysenbach et al., 2021; Chen et al., 2021). These reward learning approaches have shown successes in real-world robotic manipulation tasks from high-dimensional image inputs (Finn et al., 2016; Singh et al., 2019; Zhu et al., 2020; Chen et al., 2021). Nevertheless, to combat covariate shift that could

lead the policy to drift away from the expert distribution, these methods usually require significant online interaction. Unlike these works that study online settings, we consider learning visuomotor skills from offline datasets.

Offline RL. Offline RL (Ernst et al., 2005; Riedmiller, 2005; Lange et al., 2012; Levine et al., 2020) studies the problem of learning a policy from a static dataset without online data collection in the environment, which has shown promising results in robotic manipulation (Kalashnikov et al., 2018; Mandlekar et al., 2020; Rafailov et al., 2021; Singh et al., 2020; Julian et al., 2020; Kalashnikov et al., 2021). Prior offline RL methods focus on the challenge of distribution shift between the offline training data and deployment using a variety of techniques, such as policy constraints (Fujimoto et al., 2018; Liu et al., 2020; Jaques et al., 2019; Wu et al., 2019; Zhou et al., 2020; Kumar et al., 2019; Siegel et al., 2020; Peng et al., 2019; Fujimoto and Gu, 2021; Ghasemipour et al., 2021), conservative Q-functions (Kumar et al., 2020; Kostrikov et al., 2021; Yu et al., 2021; Sinha and Garg, 2021), and penalizing out-of-distribution states generated by learned dynamics models (Kidambi et al., 2020; Yu et al., 2020b; Matsushima et al., 2020; Argenson and Dulac-Arnold, 2020; Swazinna et al., 2020; Rafailov et al., 2021; Lee et al., 2021; Yu et al., 2021).

While these prior works successfully address the issue of distribution shift, they still require reward annotations for the offline data. Practical approaches have used manual reward sketching to train a reward model (Cabi et al., 2019; Konyushkova et al., 2020; Rafailov et al., 2021) or heuristic reward functions (Yu et al., 2022). Others have considered offline learning from demonstrations, without access to a predefined reward function (Mandlekar et al., 2020; Zolna et al., 2020a; Xu et al., 2022; Jarboui and Perchet, 2021), however they rely on high-quality demonstration data. In contrast, our method: (1) addresses distributional shift induced by both the learned policy and the reward function in a principled way, (2) only requires user-provided goal states and (3) does not require expert-quality data, resulting in an effective and practical offline reward learning scheme.

3. Learning to Achieve Examples Offline

Offline RL methods typically require regularization, and our method will employ regularization in two ways. First, we regularize the policy with an additional behavioral cloning term, which penalizes the policy for sampling out-of-distribution actions. Second, our method uses the Q-function for the behavioral policy, so it performs one (not many) step of policy improvement. These regularizers mean that our approach is not guaranteed to yield the optimal policy.

3.1. Preliminaries

We assume that an agent interacts with an MDP with states $s \in \mathcal{S}$, actions a , a state-only reward function $r(s) \geq 0$, initial state distribution $p_0(s_0)$ and dynamics $p(s_{t+1} | s_t, a_t)$. We use $\tau = (s_0, a_0, s_1, a_1, \dots)$ to denote an infinite-length trajectory. The likelihood of a trajectory under a policy $\pi(a | s)$ is $\pi(\tau) = p_0(s_0) \prod_{t=0}^{\infty} p(s_{t+1} | s_t, a_t) \pi(a_t | s_t)$. The objective is to learn a policy $\pi(a | s)$ that maximizes the expected, γ -discounted sum of rewards: $\max_{\pi} \mathbb{E}_{\pi(\tau)} [\sum_{t=0}^{\infty} \gamma^t r(s_t)]$. We define the Q-function for policy π as the expected discounted sum of returns, conditioned on an initial state and action:

$$Q^{\pi}(s, a) = \mathbb{E}_{\pi(\tau)} \left[\sum_{t=0}^{\infty} \gamma^t r(s_t) \middle| \begin{matrix} s_0=s \\ a_0=a \end{matrix} \right]. \quad (1)$$

We will focus on the offline (i.e., batch RL) setting. Instead of learning by interacting with the environment (i.e., via trial and error), the RL agent will receive as input a dataset of trajectories $\mathcal{D}_\tau = \{\tau \sim \beta(\tau)\}$ collected by a behavioral policy $\beta(a | s)$. We will use $Q^\beta(s, a)$ to denote the Q-function of the behavioral policy.

Specifying the reward function. In many real-world applications, specifying and measuring a scalar reward function is challenging, but providing examples of good states (i.e., those which would receive high rewards) is straightforward. Thus, we follow prior work (Fu et al., 2018b; Zolna et al., 2020a; Eysenbach et al., 2021; Xu and Denil, 2019; Zolna et al., 2020b) in assuming that the agent does not observe scalar rewards (i.e., \mathcal{D}_τ does not contain reward information). Instead, the agent receives as input a dataset $\mathcal{D}_* = \{s^*\}$ of high-reward states $s^* \in \mathcal{S}$. These high-reward states are examples of good outcomes, which the agent would like to achieve. The high-reward states are not labeled with their specific reward value.

To make the control problem well defined, we must relate these success examples to the reward function. We do this by assuming that the frequency of each success example is proportional to its reward: very good states are more likely to appear (and be duplicated) as success examples.

Assumption 1 *Let $p_\tau(s)$ be the empirical probability density of state s in the trajectory dataset, and let $p_*(s)$ as the empirical probability density of state s under the high-reward state dataset. We assume that there exists a positive constant c such that $r(s) = c \frac{p_*(s)}{p_\tau(s)}$ for all states s .*

This is the same assumption as Eysenbach et al. (2021). This assumption is important because it shows how example-based control is universal: for any reward function, we can specify the corresponding example-based problem by constructing a dataset of success examples that are sampled according to their rewards. We assumed that rewards are non-negative so that these sampling probabilities are positive.

This assumption can also be read in reverse. When a user constructs a dataset of success examples in an arbitrary fashion, they are implicitly defining a reward function. In the tabular setting, the (implicit) reward function for state s is the count of the times s occurs in the dataset of success examples. Compared with goal-conditioned RL (Kaelbling, 1993), defining tasks via success examples is more general. By identifying what all the success examples have in common (e.g., laundry is folded), the RL agent can learn what is necessary to solve the task and what is irrelevant (e.g., the color of the clothes in the laundry). We now can define our problem statement as follows:

Definition 1 *In the **offline example-based control** problem, a learning algorithm receives as input a dataset of trajectories $\mathcal{D}_\tau = \{\tau\}$ and a dataset of successful outcomes $\mathcal{D}_* = \{s\}$ satisfying Assumption 1. The aim is to output a policy that maximizes the RL objective (Eq. 3.1).*

This problem setting is appealing because it mirrors many practical RL applications: a user has access to historical data from past experience, but collecting new experience is prohibitively expensive. Moreover, this problem setting can mitigate the challenges of reward function design. Rather than having to implement a reward function and add instruments to measure the corresponding components, the users need only provide a handful of observations that solved the task. This problem setting is similar to imitation learning, in the sense that the only inputs are data. However, unlike imitation learning, in this problem setting the high-reward states are not labeled with actions, and these high-reward states may not necessarily contain entire trajectories.

An implicit model of future s . Our method will estimate the discounted state occupancy measure,

$$p^\beta(s_{t+} = s \mid s_0, a_0) = (1 - \gamma) \sum_{t=0}^{\infty} \gamma^t p_t^\pi(s_t = s \mid s_0, a_0), \quad (2)$$

where $p_t^\beta(s_t \mid s, a)$ is the probability of policy $\beta(a \mid s)$ visiting state s_t after exactly t time steps. Unlike the transition function $p(s_{t+1} \mid s_t, a_t)$, the discounted state occupancy measure indicates the probability of visiting a state at any point in the future, not just at the immediate next time step. In tabular settings, this distribution corresponds to the successor representations (Dayan, 1993). To handle continuous settings, we will use the contrastive approach from recent work (Mazouze et al., 2020; Eysenbach et al., 2022). We will learn a function $f(s, a, s_f) \in \mathbb{R}$ takes as input an initial state-action pair as well as a candidate future state, and outputs a score estimating the likelihood that s_f is a real future state. The loss function is a standard contrastive learning loss (e.g., Ma and Collins (2018)), where positive examples are triplets of a state, action, and future state:

$$\max_f \mathcal{L}(f; \mathcal{D}_\tau) = \mathbb{E}_{p(s,a), s_f \sim p^\beta(s_{t+} \mid s, a)} [\log \sigma(f(s, a, s_f))] + \mathbb{E}_{p(s,a), s_f \sim p(s)} [\log(1 - \sigma(f(s, a, s_f)))] ,$$

where $\sigma(\cdot)$ is the sigmoid function. At optimality, the implicit dynamics model encodes the discounted state occupancy measure:

$$f^*(s, a, s_f) = \log p^\beta(s_{t+} = s_f \mid s, a) - \log p_\tau(s_f). \quad (3)$$

We visualize this implicit dynamics model in Fig. 1. Note that this dynamics model is policy dependent. Because it is trained with data collected from one policy ($\beta(a \mid s)$), it will correspond to the probability that *that* policy visits states in the future. Because of this, our method will result in estimating the value function for the behavioral policy (akin to 1-step RL (Brandfonbrener et al., 2021)), and will not perform multiple steps of policy improvement. Intuitively, the training of this implicit model resembles hindsight relabeling (Kaelbling, 1993; Andrychowicz et al., 2017). However, it is generally unclear how to use hindsight relabeling for single-task problems. Despite being a single-task method, our method will be able to make use of hindsight relabeling to train the dynamics model.

3.2. Deriving Our Method

The key idea behind our method is that this implicit dynamics model can be used to represent the Q-values for the example-based problem, up to a constant.

Lemma 2 *Assume that the implicit dynamics model is learned without errors. Then the Q-function for the data collection policy $\beta(a \mid s)$ can be expressed in terms of this implicit dynamics model:*

$$Q^\beta(s, a) = \frac{c}{1 - \gamma} \mathbb{E}_{p_*(s^*)} \left[e^{f(s, a, s^*)} \right]. \quad (4)$$

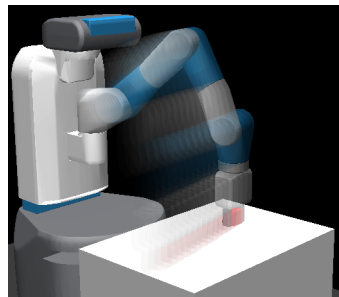


Figure 1: Our method will estimate the discounted state occupancy measure using contrastive learning. Note that this is the average over many future states.

See [Appendix](#) for the proof.

So, after learning the implicit dynamics model, we can estimate the Q-values by averaging this model’s predictions across the success examples. We will update the policy using Q-values estimated in this manner, plus a regularization term:

$$\min_{\pi} \mathcal{L}(\pi; f, \mathcal{D}_*) , \quad -(1 - \lambda) \mathbb{E}_{\pi(a|s)p(s), s^* \sim \mathcal{D}_*} \left[e^{f(s, a, s^*)} \right] - \lambda \mathbb{E}_{s, a \sim \mathcal{D}_\tau} [\log \pi(a | s)]. \quad (5)$$

In our experiments, we use a weak regularization coefficient of $\lambda = 0.5$.

It is worth comparing this approach to prior methods based on learned reward functions (Xu and Denil, 2019; Fu et al., 2018b; Zolna et al., 2020a). Those methods learn a reward function from the success examples, and use that learned reward function to synthetically label the dataset of trajectories. Both approaches can be interpreted as learning a function on one of the datasets and then applying that function to the other dataset. Because it is easier to fit a function when given large quantities of data, we predict that our approach will outperform the learned reward function approach when the number of success examples is small, relative to the number of unlabeled trajectories. Other prior methods (Eysenbach et al., 2021; Reddy et al., 2020) avoid learning reward functions by proposing TD update rules that are applied to both the unlabeled transitions and the high-return states. However, because these methods have yet to be adapted to the offline RL setting, we will focus our comparisons on the reward-learning methods.

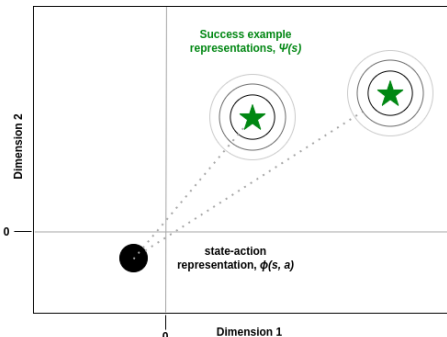


Figure 2: If the state-action representation $\phi(s, a)$ is close to the representation of a high-return state $\psi(s)$, then the policy is likely to visit that state. Our method estimates Q-values by combining the distances to all the high-return states (Eq. 1).

3.3. A Geometric Perspective

Before presenting the complete RL algorithm, we provide a geometric perspective on the representations learned by our method. Our implicit models learns a representation of state-action pairs $\phi(s, a)$ as well as a representation of future states $\psi(s)$. One way that our method can optimize these representations is by treating $\phi(s, a)$ as a prediction for the future representations.¹ Each of the high-return states can be mapped to the same representation space. To determine whether a state-action pair has a large or small Q-value, we can simply see whether the predicted representation $\phi(s, a)$ is close to the representations of any of the success examples. Our method learns these representations so that the Q-values are directly related to the Euclidean distances² from each success example. Thus, our method can be interpreted as learning a representation space such that estimating Q-values corresponds to simple geometric operations (kernel smoothing with an RBF kernel (Hastie et al., 2009, Chpt. 6)) on the learned representations. While the example-based control problem is more general than goal-conditioned RL (see Sec. 3.1), we can recover goal-conditioned RL as a special case by using a single success example.

1. Our method can also learn the opposite, where $\psi(s)$ is a prediction for the previous representations.
2. When representations are normalized, the dot product is equivalent to the Euclidean norm. We find that unnormalized features work better in our experiments.

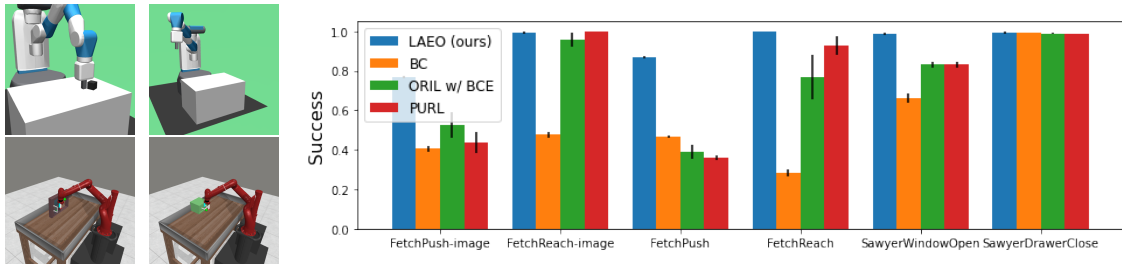


Figure 3: **Benchmark comparison:** We evaluate the performance of LAEO on six simulated manipulation tasks. FetchReach and FetchPush are two manipulation tasks from Plappert et al. (2018) that use state-based observations. FetchReach-image and FetchPush-image are the same tasks but with image-based observations. SawyerWindowOpen and SawyerDrawerClose are two state-based manipulation tasks from Yu et al. (2020a). LAEO matches or outperforms prior example-based offline RL methods on state and image-based tasks, including those that learn a separate reward function (ORIL, PURL).

3.4. A Complete Algorithm

We now build a complete offline RL algorithm based on these Q-functions. We will call our method LEARNING TO ACHIEVE EXAMPLES OFFLINE (LAEO). Our algorithm will resemble one-step RL methods, but differ in how the Q-function is trained. After learning the implicit dynamics model (and, hence, Q-function) we will optimize the policy. The objective for the policy is maximizing (log) Q-values plus a regularization term, which penalizes sampling unseen actions:³

$$\begin{aligned} \max_{\pi} (1 - \lambda) \log \mathbb{E}_{\pi(a|s)p_{\tau}(s)} [Q(s, a)] + \lambda \mathbb{E}_{(s,a) \sim p_{\tau}(s,a)} [\log \pi(a | s)] \\ = (1 - \lambda) \log \mathbb{E}_{\pi(a|s), s^* \sim p_*(s)} [e^{f(s,a,s^*)}] + \lambda \mathbb{E}_{(s,a) \sim p_{\tau}(s,a)} [\log \pi(a | s)]. \end{aligned} \quad (6)$$

As noted above, this is a one-step RL method: it updates the policy to maximize the Q-values of the behavioral policy. Performing just a single step of policy improvement can be viewed as a form of regularization in RL, in the same spirit as early stopping is a form of regularization in supervised learning. Prior work has found that one-step RL methods can perform well in the offline RL setting. Because our method performs only a single step of policy improvement, we are not guaranteed that it will converge to the reward-maximizing policy. We summarize the complete algorithm in Alg. 1.

Algorithm 1 Learning to Achieve Examples Offline

- 1: **Inputs:** dataset of trajectories $\mathcal{D} = \{\tau\}$,
dataset of high-return states $\mathcal{D}_* = \{s\}$.
 - 2: Learn the model via contrastive learning: $f \leftarrow \arg \min_f \mathcal{L}(f; \mathcal{D}_{\tau})$ ▷ Eq. 5
 - 3: Learn the policy: $\pi \leftarrow \arg \min_{\pi} \mathcal{L}(\pi; f, \mathcal{D}_*)$ ▷ Eq. 6
 - 4: **return** policy $\pi(a | s)$
-

4. Experiments

Our experiments test whether LAEO can effectively solve offline RL tasks that are specified by examples of high-return states, rather than via scalar reward functions. We study when our approach outperforms prior approaches based on learned reward functions. We look not only at the performance relative to baselines on state-based and image-based tasks, but also how that performance depends on the size and composition of the input datasets. Additional experiments study how LAEO

3. For all experiments except Fig. 7, we apply Jensen’s inequality to the first term, using $\mathbb{E}_{\pi(a|s), s^* \sim p_*(s)} [f(s, a, s^*)]$.

performs when provided with varying numbers of success observations and whether our method can solve partially observed tasks. We include full hyperparameters and implementation details in the [Appendix](#). Code is available at <https://github.com/khatch31/laeo>.

Baselines. Our main point of comparison will be prior methods that use learned reward functions: ORIL (Zolna et al., 2020a) and PURL (Xu and Denil, 2019). The main difference between these methods is the loss function used to train reward function: ORIL uses binary cross entropy loss while PURL uses a positive-unlabeled loss (Xu and Denil, 2019). Note that the ORIL paper also reports results using a positive-unlabeled loss, but for the sake of clarity we simply refer to it as PURL. After learning the reward function, each of these methods applies an off-the-shelf RL algorithm. We will implement all baselines using the TD3+BC (Fujimoto and Gu, 2021) offline RL algorithm. These offline RL methods achieve good performance on tasks specified via reward functions (Kostrikov et al., 2021; Brandfonbrener et al., 2021; Fujimoto and Gu, 2021). We also include Behavioral Cloning (BC) results.

Benchmark comparison. We start by comparing the performance of LAEO to these baselines on six manipulation tasks. FetchReach and FetchPush are two manipulation tasks from Plappert et al. (2018) that use state-based observations. FetchReach-image and FetchPush-image are the same tasks but with image-based observations. SawyerWindowOpen and SawyerDrawerClose are two manipulation tasks from Yu et al. (2020a). For each of these tasks, we collect a dataset of medium quality by training an online agent from Eysenbach et al. (2022) and rolling out multiple checkpoints during the course of training. The resulting datasets have success rates between 45% – 50%. We report results after 500,000 training gradient steps (or 250,000 steps, if the task success rates have converged by that point).

We report results in Fig. 3. We observe that LAEO, PURL, and ORIL perform similarly on FetchReach and FetchReach-image. This is likely because these are relatively easy tasks, and each of these methods is able to achieve a high success rate. Note that all of these methods significantly outperform BC, indicating that they are able to learn better policies than the mode behavior policies represented in the datasets. On SawyerDrawerClose, all methods, including BC, achieve near perfect success rates, likely due to the simplicity of this task. On FetchPush, FetchPush-image, and SawyerWindowOpen, LAEO outperforms all of the baselines by a significant margin. Recall that the main difference between LAEO and PURL/ORIL is by learning a dynamics model, rather than the reward function. These experiments suggest that for tasks with more complex dynamics, learning a dynamics model can achieve better performance than is achieved by model-free reward classifier methods.

Varying the input data. One important criterion for offline RL algorithms is that they can learn from datasets of varying quality, varying from expert-level demonstrations to low-quality data collected from a near-random policy. Our next experiment studies how the dataset composition affects LAEO and the baselines. We use three tasks: FetchReach, FetchPush, and FetchReach-image. On each of these tasks, we generate a low-quality dataset by rolling out multiple checkpoints from a partially trained agent from Eysenbach et al. (2022). In comparison to the medium-quality datasets collected earlier, which have success rates between 45% – 50%, these low quality datasets have success rates between 8% – 12%.

We report results in Fig. 4 using the FetchReach-i mage (hard) task, finding that LAEO outperforms the baselines. These results suggests that learning a dynamics model (instead of a reward function) may be especially useful in image based domains with low quality datasets.

Our next experiments study how varying the number of high-return example states and the number of reward-free trajectories affects performance. As noted in the Sec. 1, we conjecture that our method will be especially beneficial relative to reward-learning approaches in settings with very few high-return example states.

In Fig. 5 (left), we vary the number of high-return example states on FetchPush-i mage, holding the number of unlabeled trajectories constant. We observe that LAEO maintains achieves the same performance with 1 success example as with 200 success examples. In contrast, ORIL’s performance decreases as the number of high-return example states decreases. In Fig. 5 (right), we vary the number of unlabeled trajectories, holding the number of high-return example states constant at 200. We test the performance of LAEO vs. ORIL on three different dataset sizes on FetchPush-i mage, roughly corresponding to three different orders of magnitude: the $0.1\times$ dataset contains 3,966 trajectories, the $1\times$ dataset contains 31,271 trajectories, and the $10\times$ dataset contains 300,578 trajectories. We observe that LAEO continues to see performance gains as number of unlabeled trajectories increases, whereas ORIL’s performance plateaus. Taken together these results suggest that, in comparison to reward classifier based methods, LAEO needs less human supervision and is more effective at leveraging large quantities of unlabeled data.

Partial Observability. We also test the performance of LAEO on a partially-observed task. We modify the camera position in the FetchPush-i mage so that the block is occluded whenever the end effector is moved to touch the block. While such partial observability can stymie temporal difference methods (Whitehead and Ballard, 1991), we predict that LAEO might continue to solve this task because it does not rely on temporal difference learning. The results, shown in Fig. 6, confirm this prediction. On this partially observable task, we compare the performance of LAEO

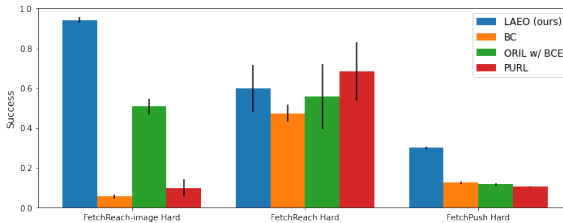


Figure 4: **Data quality.** LAEO continues to match or outperform reward classifier based methods on datasets that contain a low percentage of successful trajectories.

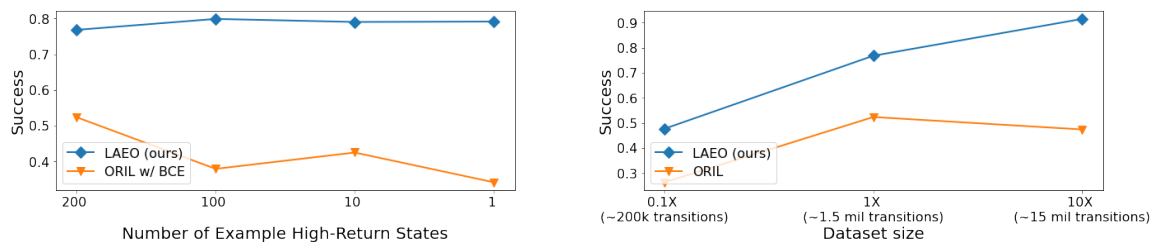


Figure 5: **Effect of dataset size:** (Left) LAEO outperforms ORIL on FetchPush-i mage when only a small number of high-return example states are given, likely because ORIL struggles to fit the learned reward function on such a small dataset. (Right) LAEO continues to improve when trained with more reward-free trajectories, while the ORIL’s performance plateaus.

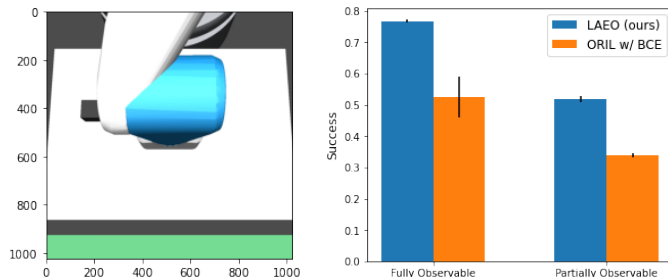


Figure 6: **Partial observability.** LAEO continues to solve the manipulation task in a setting where the new camera placement causes partial observability.

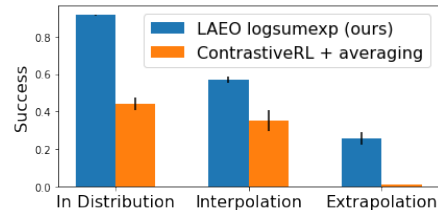


Figure 7: **Comparison with goal-conditioned RL.** LAEO solves manipulation tasks at multiple different locations without being provided with a goal-state at test time.

with that of ORIL, the best performing baseline on the fully observable tasks. On the partially observable task, LAEO achieves a success rate of 51.9%, versus 33.9% for ORIL.

Comparison to Goal-Conditioned RL. One of the key advantages of example-based control, relative to goal-conditioned RL, is that the policy can identify common patterns in the success examples to solve tasks in scenarios where it has never before seen a success example. In settings such as robotics, this can be an issue since acquiring a goal state to provide to the agent requires already solving the desired task in the first place. We test this capability in a variant of the SawyerDrawerCI ose environment. For training, the drawer’s X position is chosen as one of five fixed locations. Then, we evaluate the policy learned by LAEO on three types of environments: *In Distribution*: the drawer’s X position is one of the five locations from training; *Interpolation*: The drawer’s X position is between some of the locations seen during training; *Extrapolation*: The drawer’s X position is outside the range of X positions seen during training. We compare to a goal-conditioned policy learned via contrastive RL, where actions are extracted by averaging over the (training) success examples: $\pi(a | s) = \mathbb{E}_{s^* \sim p_*(s)}[\pi(a | s, g = s^*)]$.

The results, shown in Fig. 7, show that LAEO consistently outperforms this goal-conditioned baseline. As expected, the performance is highest for the In Distribution environments and lowest for the Extrapolation environments. Taken together, these experiments show that LAEO can learn to reach multiple different goal locations without access to goal states during test time.

5. Conclusion

In this paper, we presented an RL algorithm aimed at settings where data collection and reward specification are difficult. Our method learns from a combination of high-return states and reward-free trajectories, integrating these two types of information to learn reward-maximizing policies. Whereas prior methods perform this integration by learning a reward function and then applying an off-the-shelf RL algorithm, ours learns an implicit dynamics model. Not only is our method simpler (no additional RL algorithm required!), but also it achieves higher success rates than prior methods.

While our experiments only start to study the ability of contrastive-based methods to scale to high-dimensional observations, we conjecture that methods like LAEO may be particularly amenable to such problems because the method for learning the representations (contrastive learning) resembles prior representation learning methods (Mazouze et al., 2020; Nair et al., 2022). Scaling this method to very large offline datasets is an important direction for future work.

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