In this supplementary material, we provide the pseudocode of two unlearning methods, Projected Gradient Ascent (PGA) (Halimi et al., 2022) and FedEraser (Liu et al., 2021) in Section A. Next, we provide the experimental setting and results of our experiments on CIFAR-100 in Section B.

Appendix A. FedUnlearn Method

A.1. Projected Gradient Ascent (PGA)

The natural approach to unlearning involves updating the model parameters in the opposite direction of the loss function gradient. However, simply maximizing the loss using gradient ascent can pose problems, particularly when the loss is unbounded, as is often the case with, for instance, the cross-entropy loss. In situations with an unbounded loss, each gradient step leads toward a model that increases the loss, and after several steps, it may converge to an arbitrary, random-like model.

To tackle this challenge, PGA (Halimi et al., 2022) projects the updated model parameters onto a ball centered at the reference model parameters. These reference model parameters are calculated as the average of the model parameters of all clients except the removed client. The projection ensures that the updated model parameters remain close to the reference model parameters. The pseudocode for PGA can be found in Algorithm 1.
Algorithm 1 Unlearning via Projected Gradient Ascent (Halimi et al., 2022)

Unlearning Parameters: learning rate $\eta_u$, batch size $B_u$, number of epochs $E_u$, clipping radius $\delta$, and early stopping threshold $\tau$

Split dataset $D_i$ into train set $D^{tr}_i$ and validation set $D^{val}_i$.

Set $w_{ref} \leftarrow \frac{1}{N-1} \left( Nw^T - w_i^{T-1} \right) = \frac{1}{N-1} \sum_{i \neq j} w_j^{T-1}$

Define $\mathcal{P}(w)$ as the projection of $w \in \mathbb{R}^d$ onto the $\ell_2$-norm ball $\Omega = \{ v \in \mathbb{R}^d : ||v - w_{ref}|| \leq \delta \}$

Initialize unlearning model as $w \leftarrow w_i^{T-1}$

$D_i \leftarrow$ (split $D_i^{tr}$ into batches of size $B_u$)

for each local epoch $e = 1$ to $E_i$ do
  for batch $b$ in $D_i$ do
    $w \leftarrow \mathcal{P}(w + \eta_u \nabla F^u_i(w; b))$
    if Accuracy$(w; D^{val}_i) < \tau$ then
      Set $w_i^u \leftarrow w$ and return $w_i^u$ to server
    end if
  end for
end for

Set $w_i^u \leftarrow w$ and return $w_i^u$ to server

A.2. FedEraser

To efficiently eliminate the influence of a target client’s data from the trained global model without retraining from scratch, the central server in FedEraser (Liu et al., 2021) retains client updates at regular intervals during the global model’s training process. These retained updates include the index of the corresponding round. Subsequently, the server uses this information to calibrate the retained updates, enabling the reconstruction of the unlearned global model. FedEraser follows a four-step process:

- **Step 1: Calibration Training** — This step is executed on the client’s side. Each client initializes its local model with the retained updates and subsequently trains it for a few epochs using its own dataset.

- **Step 2: Update Calibrating** — On the central server, the retained updates undergo calibration. This process utilizes the calibrated local models from each client to refine the retained updates.

- **Step 3: Calibrated Update Aggregating** — The server aggregates the calibrated updates, forming the basis for constructing the unlearned global model.

- **Step 4: Unlearned Model Updating** — The unlearned global model is updated based on the aggregated calibrated updates.

It is important to highlight that the first step is executed by individual clients (excluding the removed clients), while the subsequent stages are conducted on the server. For a more comprehensive understanding of the FedEraser implementation, please consult the pseudocode outlined in Algorithm 2.
Algorithm 2 Unlearning via FedEraser (Liu et al., 2021)

Require: Initial global model $M_1$; retained client updates $U$

Require: Target client index $k_n$

Require: Number of global calibration round $T$

Require: Number of local calibration training epoch $E_{cali}$

Central server executes:

for each round $R_{t_j}, j \in \{1, 2, ..., T\}$ do

for each client $C_{k_c}, k_c \in \{1, 2, ..., K\}$ in parallel do

$\tilde{U}_{t_j}^{k_c} \leftarrow \text{CaliTrain} \left( C_{k_c}, \tilde{M}_{k_c}^{t_j}, E_{cali} \right)$

$\tilde{U}_{k_c}^{t_j} \leftarrow \frac{|U_{t_j}^{k_c}|}{\|U_{t_j}^{k_c}\|} \tilde{U}_{t_j}^{k_c}$;

▷ Update Calibrating

end for

$\tilde{U}_{t_j}^{t_j} \leftarrow \frac{1}{(K-1)} \sum w_{k_c} \sum_{k_c} w_{k_c} \tilde{U}_{t_j}^{k_c}$;

end for

$\tilde{M}_{t_j+1} \leftarrow \tilde{M}_{t_j} + \tilde{U}_{t_j}^{t_j}$;

▷ Update Aggregating

end for

CaliTrain $\left( C_{k_c}, \tilde{M}_{k_c}^{t_j}, E_{cali} \right)$ // Run on client $C_{k_c}$

for each local training round $j$ from 1 to $E_{cali}$ do

$\tilde{M}_{k_c}^{t_j+1} \leftarrow \text{Train} \left( \tilde{M}_{k_c}^{t_j+1}, D_{k_c} \right)$

end for

$\tilde{U}_{k_c}^{t_j} \leftarrow \text{Calculation Update} \left( \tilde{M}_{k_c}^{t_j+1}, E_{cali}, M_{k_c}^{t_j+1} \right)$

return $\tilde{U}_{k_c}^{t_j}$ to the central server

Appendix B. Additional experiments on CIFAR-100

B.1. Experimental setup

Additional experiments were conducted using CIFAR-100, applying the same experimental setup as for the MNIST and CIFAR-10 datasets. The federated learning (FL) training configuration comprised five clients with an independent and identically distributed (IID) data distribution. For these experiments, backdoor samples were introduced into the training data of the removed client (client 0) at a backdoor ratio of 0.9. The trigger pattern used consisted of a 3x3 square with fixed pixel values in the bottom right corner. The backdoor label was set to 99 (with a label set of 0-99). We provided the detailed hyperparameters in Table 1.

B.2. Experimental Analysis and Discussion

In this section, we provide experiment results on CIFAR-100. In general, the results are consistent with our main analysis with MNIST and CIFAR-10.
Table 1: Hyperparameters for Three Scenarios in the FedUnlearn Setup on CIFAR-100

<table>
<thead>
<tr>
<th>Hyperparameter</th>
<th>Scenario 1</th>
<th>Scenario 2</th>
<th>Scenario 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>FL communication rounds</td>
<td>100</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td>Unlearning rounds</td>
<td>10</td>
<td>10</td>
<td>2</td>
</tr>
<tr>
<td>Post-unlearning rounds</td>
<td>30</td>
<td>30</td>
<td>30</td>
</tr>
<tr>
<td>Returning rounds</td>
<td>30</td>
<td>30</td>
<td>30</td>
</tr>
</tbody>
</table>

Figure 1: The effectiveness of unlearning methods compared to the Retrain (baseline) in three scenarios.

**RQ1: What are the impacts of different unlearning methods on CIFAR-100 dataset?**

In particular, Figs 1(a) and 1(d) depict the impact of various unlearning methods on CIFAR-100. Notably, the PGA, FedEraser, and Flipping methods demonstrate their ability to significantly reduce backdoor accuracy while maintaining a strong performance on clean data before the beginning of Post-unlearning rounds. Considering the detailed accuracy of the global model on both clean and backdoor test sets, as presented in Table 2, it becomes evident that the “Continue to Train” method is not as effective. It exhibits a slower reduction in backdoor accuracy when compared to other methods such as FedEraser, PGA, and Flipping.
Table 2: The effectiveness of four unlearning methods compared to Retrain (baseline).

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Method</th>
<th>CA BA</th>
<th>CA BA</th>
<th>CA BA</th>
<th>CA BA</th>
<th>CA BA</th>
<th>CA BA</th>
<th>CA BA</th>
<th>CA BA</th>
</tr>
</thead>
<tbody>
<tr>
<td>CIFAR-100</td>
<td>Retrain</td>
<td>0.428</td>
<td>0.009</td>
<td>0.429</td>
<td>0.009</td>
<td>0.429</td>
<td>0.009</td>
<td>0.428</td>
<td>0.009</td>
</tr>
<tr>
<td></td>
<td>ConTrain</td>
<td>0.331</td>
<td>0.946</td>
<td>0.410</td>
<td>0.788</td>
<td>0.419</td>
<td>0.559</td>
<td>0.418</td>
<td>0.538</td>
</tr>
<tr>
<td></td>
<td>PGA</td>
<td>0.331</td>
<td>0.946</td>
<td>0.272</td>
<td>0.000</td>
<td>0.305</td>
<td>0.000</td>
<td>0.418</td>
<td>0.009</td>
</tr>
<tr>
<td></td>
<td>Flipping</td>
<td>0.331</td>
<td>0.946</td>
<td>0.331</td>
<td>0.946</td>
<td>0.099</td>
<td>0.000</td>
<td>0.213</td>
<td>0.002</td>
</tr>
</tbody>
</table>

**BU**: Before Unlearning, **SU**: Start Unlearning, **FU**: Finish Unlearning, **SPU**: Start Post Unlearning, **FPU**: Finish Post Unlearning, **SR**: Start Returning, **FR**: Finish Returning

Table 3: Comparative Analysis of Unlearning Time (in seconds) among Five Methods across Three Scenarios on CIFAR-100 dataset

<table>
<thead>
<tr>
<th>Scenario</th>
<th>1</th>
<th>2</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Retrain</td>
<td>6719.94(1.00x)</td>
<td>1376.75(1.00x)</td>
<td>1369.64(1.00x)</td>
</tr>
<tr>
<td>Continue to Train</td>
<td>1276.34(5.27x)</td>
<td>1306.08(1.05x)</td>
<td>185.82(7.37x)</td>
</tr>
<tr>
<td>PGA</td>
<td>218.51(30.75x)</td>
<td>207.39(6.64x)</td>
<td>23.62(57.98x)</td>
</tr>
<tr>
<td>FedEraser</td>
<td>1220.09(5.51x)</td>
<td>1229.05(1.12x)</td>
<td>157.61(8.69x)</td>
</tr>
<tr>
<td>Flipping</td>
<td>1595.61(4.21x)</td>
<td>1610.73(0.85x)</td>
<td>324.55(4.22x)</td>
</tr>
</tbody>
</table>

1: Late unlearning 2: Early unlearning 3: Early unlearning with small unlearning rounds

**RQ2:** How early and late unlearning affect the general performance of the unlearning methods?

Figs. 1(b), 1(e), 1(c), and 1(f) demonstrate that the performance of the unlearning methods can be influenced by the communication round at which we initiate the unlearning process, as well as the number of unlearning rounds. Specifically, while the PGA and Flipping methods exhibit a reduction in backdoor accuracy during unlearning rounds, they are not as effective as the FedEraser method in all scenarios. Regarding clean accuracy, the PGA, Flipping, and FedEraser methods can maintain clean accuracy after the unlearning process.

**RQ3:** How effectively does each method facilitate returning clients?

As depicted in Fig. 1, only PGA and Flipping methods enable rapid recovery, while FedEraser requires more training rounds to achieve comparable backdoor accuracy.

**Efficiency Analysis**

**Unlearning Time.** Regarding efficiency, Table 3 reflects the same findings as our experiments with MNIST and CIFAR-10. In all scenarios, PGA is the fastest method, while unlearning with Flipping can be slower than the baseline method. This reduced speed can be attributed to the small number of FL training rounds and the significant number of unlearning rounds.
Examining the Cosine Similarity between the unlearned and baseline models, as illustrated in Fig. B.2, during the unlearning rounds, FedEraser causes the unlearned model’s behavior to diverge significantly from that of the baseline model. This divergence occurs because FedEraser updates the global model based on historical client models at interval rounds. However, starting from the post-unlearning rounds, PGA, Flipping, and FedEraser methods maintain a stable Cosine Similarity around 0.9. This suggests their convergence to align the unlearned model’s behavior with that of the baseline model, consistent with our MNIST and CIFAR-10 results.

References
