# Decouple then Combine: A Simple and Effective Framework for Fraud Transaction Detection

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#### Abstract

With the popularity of electronic mobile and online payment, the demand for detecting financial fraudulent transactions is increasing. Although numerous efforts are devoted to tackling this problem, there are still two key challenges that are not well resolved, *i.e.*, the class imbalance ratio of test samples are extremely larger than that of training samples and amount of detected fraudulent transactions do not be considered. In this paper, we propose a simple and effective framework composed of majority and minority branches to address the above issues. The input samples of majority and minority branches come from vanilla and re-adjusted distribution, respectively. Parameters of each branch are optimized individually, by which the representation learning for majority and minority samples are decoupled. Besides, an extra loss re-weighted by amount is added in the majority branch to improve the recall amount of detected fraudulent transactions. Theoretical results show that under the proposed framework, minimizing the empirical risk is guaranteed to achieve small generalization risk on more imbalanced data with high probability. Experiments on real-world datasets from Tencent Wechat payments demonstrate that our framework achieves superior performance than competitive methods in terms of both number and money of detected fraudulent transactions.

Keywords: Imbalance Learning, Fraud Detection, Tabular Data

## 1. Introduction

With rapid development of digital economy, mobile payments have been integrated into people's daily lives. Accompanied by the widespread popularity of mobile payments, the occurrences of fraudulent transactions also increase significantly, resulting in large quantities amounts loss of users (Lin et al., 2021; Liu et al., 2021b,a). Therefore, financial fraud

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detection has drawn increasing attention in recent years. There are two main tasks in financial fraud detection, *i.e.*, user-oriented task and transaction-oriented task. The former aims to judge whether a user is fraudulent or benign. The latter aims to distinguish fraudulent transactions from numerous transactions. In this work, we focus on the latter one. Both user-oriented and transaction-oriented financial detection tasks can be abstracted as imbalance classification (He and Garcia, 2009), one of the most fundamental but challenging problems in machine learning and data mining. Existing methods for imbalance classification generally fall into re-sampling approaches (Batista et al., 2004; Peng et al., 2019; Liu et al., 2020a), re-weighting approaches (Ren et al., 2018; Shu et al., 2019; Hu et al., 2019), ensemble learning approaches (Wang and Yao, 2009; Galar et al., 2013; Liu et al., 2020b), cost-sensitive learning approaches (Karakoulas and Shawe-Taylor, 1998; Fan et al., 1999), AUC optimization approaches (Qi et al., 2021; Yang et al., 2021), to name a few.

Although the above studies have made great progress in tackling the class imbalance problem, it is not trivial to apply them on real financial fraudulent detection scenarios. We emphasize the following three additional challenges. First, the number of fraudulent transactions is *extremely* smaller than that of benign transactions in real scenarios. Concretely, there is only one fraudulent transaction in millions of transactions. However, the ratio of majority to minority is commonly in the order of hundreds in previous studies. The extreme imbalance ratio seriously affects their effectiveness. Second, previous works (Cui et al., 2019; Cao et al., 2019; Shu et al., 2019) assume that class imbalance lies only in the training data. However, in real financial detection tasks, both training and test samples are class-imbalanced, and the test set has an even higher class-imbalance ratio than training data, due to the number of frauds will decrease under interception from online anti-fraud system. Third, the amounts vary by transaction, and it is required that the amounts of detected fraud transactions are as large as possible. Unfortunately, previous works only consider the number of recalled fraudulent transactions, leading to the model failing to discover some fraudulent transaction with large amounts. Besides, the data of payment transactions is commonly presented in tabular form, which is much more challenging than both image (Lin et al., 2017; Cui et al., 2019; Zhou et al., 2020) and graph-structured data (Lin et al., 2021; Liu et al., 2021b,a).

To overcome these challenges, in this paper, we propose a simple but effective method for detecting fraudulent transactions. We empirically found that re-weighting and re-balanced methods fail to handle the real-application data. Inspired by the conventional branch proposed in recent work (Zhou et al., 2020), our model is composed of majority-level and minority-level branches, which receive data from vanilla distribution and re-adjusted distribution, respectively. Since majority samples are dominant in vanilla distribution, the majority-level branch focuses on learning representations of majority samples. Differently, the minority samples are over-sampled in a re-adjusted distribution, by which the minority become dominant. It is worth mentioning that sharing weights in (Zhou et al., 2020) limit the representation ability of model, particularly on tabular data. To this end, the parameters of all branches are updated individually, so that the representations from majority and minority branch to improve the recall rate of amounts. After that, representations from different branches are aggregated via learnable weights to obtain the final prediction. Surprisingly, this simple model obtains superior performance on real-world data, which sheds

light on addressing this challenging issue for an industrial circle. Experiments are conducted on real-world datasets from Tencent Wechat payments, one of the largest electronic mobile and online payment platforms. The proposed framework significantly outperforms other competitive baselines. The main contributions of this work are summarized as follows:

- We propose to decouple the representation learning of majority and minority samples, which is simple to implement and empirically shown to be effective in addressing the extreme class imbalance problem.
- We provide a theoretical analysis on the proposed framework, which demonstrates that the proposed framework can achieve a small generalization risk on data with a higher class-imbalanced ratio.
- Experimental results on real-world data from Tencent Wechat payments verify the effectiveness of the proposed method.

# 2. Problem Formulation

Let  $\mathcal{X}$  denote the feature space,  $\mathcal{Y} = \{0, 1\}$  denote the space of class labels, and  $\mathcal{M} \in \mathbb{R}_+ \cup \{0\}$  denote the space of transactions amounts. The training set  $\widehat{\mathcal{D}} = \{(\boldsymbol{x}_i, y_i, m_i)\}_{i=1}^N$  is drawn from the distribution  $\mathcal{D}$  over  $\mathcal{X} \times \mathcal{Y} \times \mathcal{M}$ . For a transaction  $(\boldsymbol{x}_i, y_i, m_i)$ , the label  $y_i = 0$  means it is benign while the label  $y_i = 1$  means it is fraudulent, where  $m_i$  is the amount of this transaction.  $m_i > 0$  when  $y_i = 1$  and  $m_i = 0$  when  $y_i = 0$ . Denote  $\mathbb{I}(\cdot)$  as the indicator function. In our work, we consider the real-world fraudulent transaction detection, where the number of fraudulent payments is much less than the number of benign payments, *i.e.*,

$$\frac{\sum_{(\boldsymbol{x}_i, y_i, m_i) \in \widehat{D}} \mathbb{I}(y_i = 0)}{\sum_{(\boldsymbol{x}_i, y_i, m_i) \in \widehat{D}} \mathbb{I}(y_i = 1)} \gg 1.$$
(1)

**Evaluation Metrics.** Let  $c(\boldsymbol{x}; \theta) \in [0, 1]$  denote a classifier parameterized by  $\theta$ , which outputs a score measuring whether a payment is fraudulent. In real-world scenarios, to keep users from being defrauded, fraud detection can tolerate a certain number of benign payments being misclassified as fraudulent payments. Thus, the ratio of detected fraudulent payments to total fraudulent payments is commonly chosen as the evaluation metric. Due to the large scale of the payments, we can only focus on a small portion of the payments whose scores rank in the top. In our work, we use  $P_K$  and  $A_K$  as metrics, which are defined by:

$$P_K = \frac{\sum_{(\boldsymbol{x}_i, y_i) \in t(K)} y_i}{\sum_{(\boldsymbol{x}_i, y_i) \in \widehat{\mathcal{D}}_{\text{test}}} y_i},\tag{2}$$

$$A_K = \frac{\sum_{(\boldsymbol{x}_i, y_i, m_i) \in t(K)} m_i}{\sum_{(\boldsymbol{x}_i, y_i, m_i) \in \widehat{\mathcal{D}}_{\text{test}}} m_i},\tag{3}$$

where  $\widehat{\mathcal{D}}_{\text{test}} = \{ \boldsymbol{x}_i, y_i, m_i \}_i^M$  denotes the test dataset.  $t(K) \in \widehat{\mathcal{D}}_{\text{test}}$  denotes the subset of the test set whose scores rank in the top K:

$$t(K) = \left\{ (\boldsymbol{x}_i, y_i, m_i) | (\boldsymbol{x}_i, y_i, m_i) \in \widehat{\mathcal{D}}_{\text{test}}, c(\boldsymbol{x}_i; \theta) > \widehat{s}_K \right\},$$
(4)



Figure 1: Illustration of the bi-collaborative learning framework. The green (orange) color denote the majority (minority) branch receiving samples from vanilla (re-adjusted) distribution.

where  $\hat{s}_K$  is exactly the K-th largest score in  $\{c(\boldsymbol{x}_i; \theta)\}_i^M, \boldsymbol{x}_i \in \widehat{\mathcal{D}}_{\text{test}}.$ 

Note that in real-world scenarios, test set is still imbalanced, which is contrary to plenty of existing literature of imbalance learning (Cui et al., 2019; Cao et al., 2019; Shu et al., 2019). Thus, Equation (1) still holds in test set.

# 3. Our Proposed Method

In this section, we detail our proposed method, including data samplers, bi-collaborative learning framework, tri-collaborative learning framework and inference phase.

#### 3.1. Data Samplers

In Figure 1, we visualize the bilateral branches framework for our bilateral collaborative learning method (BiCo). The two branches achieve different functions in imbalance learning via different data samplers. The majority branch adopts a instance-uniform data sampler for representation learning, while the minority branch adopts a class-reversed data samplers for re-balancing learning. The collaborative learning of these bilateral branches with different data samplers facilitates the learning in imbalanced scenarios.

First, we introduce the two data samplers in Figure 1, *i.e.*, instance-uniform data sampler and class-reversed data sampler. Recently, some literature show that in imbalance learning, using the cross entropy loss function over the original given imbalanced training dataset can lead to better semantic representation (Zhou et al., 2020; Yuan et al., 2021) as it can retain the original characteristics of the training data. The instance-uniform data samplers adopt the same distribution as the original training data. It is termed "instance-uniform data samplers" because it is equivalent to sampling each instance with same probability.

However, in imbalance training dataset, the "head" class dominates the loss function, making the classifier not pay enough attention to the "tail" class. Therefore, we introduce the class-reversed data sampler, which samples more "tail" class (fraudulent payments) than "head" class (benign payments). The class-reversed data sampler reverses the sampling probability of the benign payments and fraudulent payments in training dataset. Let  $N_0$  denote the number of benign payments and  $N_1$  denote the number of fraudulent payments in the original training dataset. The class-reversed data sampler samples benign transactions with probability  $\frac{N_1}{N_0+N_1}$  and samples fraudulent transactions with probability  $\frac{N_0}{N_0+N_1}$ .

#### 3.2. Bi-Collaborative Learning Framework

Next, we elaborate the details of our bilateral branch framework for collaborative learning in Fraud transaction detection, which is termed BiCo. Both the upper branch and the lower branch are firstly fed to a multi-layer perceptron (MLP), which outputs two different feature representations. Let  $(\boldsymbol{x}_u, y_u, m_u)$  and  $(\boldsymbol{x}_c, y_c, m_c)$  denote the data generated by instanceuniform sampler and class-revversed sampler, respectively. Let  $f_u(\boldsymbol{x}_u) \in \mathbb{R}^D$  denote the representation from instance-uniform data sampler (upper branch) and  $f_c(\boldsymbol{x}_c) \in \mathbb{R}^D$  denote the representation from class-reversed data sampler (lower branch). These two MLPs adopt the same network architecture but do not share weights, which is one of key differences between BiCo and BBN (Zhou et al., 2020).

Furthermore, we propose a simple but effective approach to achieve collaborative learning of two branches. We introduce two mixed weights  $\boldsymbol{w}_u \in \mathbb{R}^D$  and  $\boldsymbol{w}_c \in \mathbb{R}^D$  to integrate  $f_u(x_u)$  and  $f_c(x_c)$ . Then, we get the final mixed logit by a simple element addition, which is formulated as

$$z = \boldsymbol{w}_u^{\top} f_u(\boldsymbol{x}_u) + \boldsymbol{w}_c^{\top} f_c(\boldsymbol{x}_c), \qquad (5)$$

where  $z \in \mathbb{R}$  is the mixed logit. We adopt sigmoid function to calculate the predicted scores

$$s = \frac{1}{1 + \exp(-z)}.$$
 (6)

Then, the loss function of the proposed framework for collaborative learning is defined by

$$\mathcal{L} = l_{ce}(s, y_u) + l_{ce}(s, y_c), \tag{7}$$

where  $l_{ce}$  is the cross-entropy loss function:

$$l_{ce}(s,y) = -[ylog(s) + (1-y)log(1-s)].$$
(8)

We adopt the mini-batch gradient descent to optimize the parameters of the two MLPs and the two mixed weights simultaneously.

In some real-world application scenarios, we are supposed to care more about the amount of the detected fraudulent payments  $(P_K)$  but not the number of the detected fraudulent payments, *i.e.*,  $A_K$ . A simple approach is to adopt the amounts as the coefficients for the cross-entropy loss function of the fraudulent payments, which is formulated as

$$l_{ce}^{m} = -[m \cdot y log(s) + (1 - y) log(1 - s)].$$
(9)

Thus, the loss function for increasing total amount of detected fraudulent payments is

$$\mathcal{L}^{m} = l_{ce}^{m_{u}}(s, y_{u}) + l_{ce}^{m_{c}}(s, y_{c}).$$
(10)

The bi-collaborative learning framework with Equation (10) is termed BiCo-A.



Figure 2: Illustration of the tri-collaborative learning framework. Compared with Figure 1, an extra branch denoted by blue is added to improve the amount of detected fraudulent payments.

#### 3.3. Tri-collaborative Learning Framework

Although the use of the improved loss function  $\mathcal{L}^m$  is effective for increasing  $A_k$ , it undermines the representation learning via original cross-entropy loss function, which hurts the capability of identifying detected fraudulent payments. To improve  $P_K$  and  $A_K$  simultaneously is a very challenging problem. To address this challenge, we propose the Tri-collaborative Learning Framework (TriCo) on top of BiCo, as shown in Figure 2.

In Figure 2, we adopt two data samplers, including instance-uniform data sampler and class-reversed data sampler, which is the same as the data samplers in BiCo. However, contrary to BiCo, the instance-uniform data sampler is adopted by two branches, *i.e.*, the upper branch and the middle branch. The upper branch of TriCo plays the same role as the upper branch of BiCo, which aims to learn good semantic representation via instance-uniform data sampler. The lower branch of TriCo is also the same the lower branch of BiCo. The middle branch is the difference between TriCo and BiCo. The mixed logit in the trilateral branch framework is defined as

$$z = \boldsymbol{w}_u^{\top} f_u(\boldsymbol{x}_u) + \boldsymbol{w}_a^{\top} f_a(\boldsymbol{x}_u) + \boldsymbol{w}_c^{\top} f_c(\boldsymbol{x}_c), \qquad (11)$$

where  $\boldsymbol{w}_u, \boldsymbol{w}_a, \boldsymbol{w}_c \in \mathbb{R}^D$  are the mixed weights of the upper branch, the middle branch and the lower branch, respectively.

On top of the overall loss function Equation (8) used in BiCo, we add a sub loss function, which is related to the middle branch. The middle branch aims to increase  $A_K$ . Thus, the middle branch adopt the improved cross-entropy loss function weighted by the amount of the fraudulent payments, i.e., Equation (9).

To summarize, the overall loss function adopted by TriCo is formulated as

$$\mathcal{L}^{Tri} = l_{ce}(s, y_u) + l_{ce}(s, y_c) + l_{ce}^{m_u}(s, y_u).$$
(12)

#### 3.4. Inference Phase

For the bi-collaborative learning framework, during inference phase, the two branches are fed to the same input test data. It finally outputs a mixed logit with the information of feature  $f_u$  and  $f_c$ . Thus, through original feature and re-balancing feature, the network can assign the fraudulent payments high scores.

For the tri-collaborative learning framework, during inference phase, the three branches are also fed to the same input test data. With original feature, re-balancing feature and the feature of increasing  $A_K$ , the network can also give the fraudulent payments high scores. Moreover, when only considering the fraudulent payments, the network can give fraudulent payments with more amount higher scores.

#### 3.5. Theoretical Analysis

In this part, we provide theoretical analysis to the proposed framework. Without loss of generality, the analysis is oriented to BiCo whose loss function is given by Equation (7). Denote  $\mathcal{D}_u$  and  $\mathcal{D}_c$  the samples distribution of instance-uniform and class-reversed sampler. The training samples  $(\boldsymbol{x}_u, y_u)$  and  $(\boldsymbol{x}_c, y_c)$  are drawn independently from the joint distribution  $\mathcal{D}_u \times \mathcal{D}_c$ . Denote by  $p = \frac{N_0}{N_1 + N_0}$  the probability that  $(\boldsymbol{x}_u, y_u)$  is benign in training sets, *i.e.*,  $\Pr\{y_u = 1\} = p$ . Let  $\boldsymbol{x}_+ \sim \mathcal{D}_+$  and  $\boldsymbol{x}_- \sim \mathcal{D}_-$  be the fraudulent (positive) and benign (negative) samples, respectively.  $\mathcal{D}_+$  and  $\mathcal{D}_-$  are the distribution of positive and negative samples.

**Theorem 1** Minimizing the loss defined in Equation (7) is guarantee to achieve a small generalization risk on more imbalanced data with high probability.

### **Proof** Denote by

$$\mathbb{E}_{(\boldsymbol{x}_u, y_u), (\boldsymbol{x}_c, y_c) \sim \mathcal{D}_u \times \mathcal{D}_c} \left[ \mathcal{L}(\boldsymbol{x}_u, y_u, \boldsymbol{x}_c, y_c) \right]$$

the expectation of Equation (7). We have

$$\begin{split} & \mathbb{E}_{(\boldsymbol{x}_{u},y_{u}),(\boldsymbol{x}_{c},y_{c})\sim\mathcal{D}_{u}\times\mathcal{D}_{c}}\left[\mathcal{L}(\boldsymbol{x}_{u},y_{u},\boldsymbol{x}_{c},y_{c})\right] \\ &= 2p(1-p)\mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}}\left[\log\left(1+e^{-z_{u}(\boldsymbol{x}_{+})-z_{c}(\boldsymbol{x}_{+})}\right)\right] \\ &+p^{2}\mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}}\left[\log\left(1+e^{-z_{u}(\boldsymbol{x}_{+})-z_{c}(\boldsymbol{x}_{-})}\right)+\log\left(1+e^{z_{u}(\boldsymbol{x}_{+})+z_{c}(\boldsymbol{x}_{-})}\right)\right] \\ &+(1-p)^{2}\mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}}\left[\log\left(1+e^{z_{u}(\boldsymbol{x}_{-})+z_{c}(\boldsymbol{x}_{+})}\right)+\log\left(1+e^{-z_{u}(\boldsymbol{x}_{-})-z_{c}(\boldsymbol{x}_{+})}\right)\right] \\ &+2p(1-p)\mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}}\left[\log\left(1+e^{z_{u}(\boldsymbol{x}_{-})+z_{c}(\boldsymbol{x}_{-})}\right)\right] \\ &\geq 2p(1-p)\mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}}\left[\log\left(1+e^{-z_{u}(\boldsymbol{x}_{-})+z_{c}(\boldsymbol{x}_{-})}\right)\right] \\ &+2p(1-p)\mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}}\left[\log\left(1+e^{z_{u}(\boldsymbol{x}_{-})+z_{c}(\boldsymbol{x}_{-})}\right)\right] \\ &+2\left(p^{2}+(1-p)^{2}\right)\log 2, \end{split}$$

where  $z_u(\boldsymbol{x}_+) = \boldsymbol{w}_u^{\top} f_u(\boldsymbol{x}_+)$ ,  $z_u(\boldsymbol{x}_-) = \boldsymbol{w}_u^{\top} f_u(\boldsymbol{x}_-)$ ,  $z_c(\boldsymbol{x}_+) = \boldsymbol{w}_c^{\top} f_c(\boldsymbol{x}_+)$ , and  $z_c(\boldsymbol{x}_-) = \boldsymbol{w}_c^{\top} f_c(\boldsymbol{x}_-)$ . Denote by p' the probability that (x, y) is benign in test sets, *i.e.*,  $\Pr\{y = 1\} = p'$ . As we have mentioned, p' < p holds in real-world financial fraudulent detection scenarios. Note that in the interference phase, both the majority and minority branch receive the same samples. Thus, the generalization risk is

$$\mathbb{E}_{(x,y)} \left[ \mathcal{L}(\boldsymbol{x}, y, \boldsymbol{x}, y) \right]$$
  
= $p' \mathbb{E}_{\boldsymbol{x}_+, \boldsymbol{x}_-} \left[ \log \left( 1 + e^{-z_u(\boldsymbol{x}_+) - z_c(\boldsymbol{x}_+)} \right) \right]$   
+  $(1 - p') \mathbb{E}_{\boldsymbol{x}_+, \boldsymbol{x}_-} \left[ \log \left( 1 + e^{z_u(\boldsymbol{x}_-) + z_c(\boldsymbol{x}_-)} \right) \right].$ 

Therefore, we have

$$\mathbb{E}_{(x_{u},y_{u}),(x_{c},y_{c})} \left[ \mathcal{L}(\boldsymbol{x}_{u},y_{u},\boldsymbol{x}_{c},y_{c}) \right]$$

$$> 2p'(1-p') \mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}} \left[ \log \left( 1 + e^{-z_{u}(\boldsymbol{x}_{+}) - z_{c}(\boldsymbol{x}_{+})} \right) \right] + 2 \left( p^{2} + (1-p)^{2} \right) \log 2$$

$$+ 2p'(1-p') \mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}} \left[ \log \left( 1 + e^{z_{u}(\boldsymbol{x}_{-}) + z_{c}(\boldsymbol{x}_{-})} \right) \right]$$

$$\geq 2p' \mathbb{E}_{\boldsymbol{x}_{+},\boldsymbol{x}_{-}} \left[ p' \log \left( 1 + e^{-z_{u}(\boldsymbol{x}_{+}) - z_{c}(\boldsymbol{x}_{+})} \right)$$

$$+ (1-p') \log \left( 1 + e^{z_{u}(\boldsymbol{x}_{-}) + z_{c}(\boldsymbol{x}_{-})} \right) \right] + 2 \left( p^{2} + (1-p)^{2} \right) \log 2$$

$$> 2p' \mathbb{E}_{(x,y)} \left[ \mathcal{L}(\boldsymbol{x},y,\boldsymbol{x},y) \right].$$

Thus, the expectation of  $\mathcal{L}$  on test samples is the lower bound of the expectation of  $\mathcal{L}$  on training samples, when neglecting the constant coefficient. According to the generalization analysis in (Mohri et al., 2018), the expectation term  $\mathbb{E}_{(x_u,y_u),(x_c,y_c)}[\mathcal{L}(\boldsymbol{x}_u,y_u,\boldsymbol{x}_c,y_c)]$  can be upper bounded by the training loss  $\mathcal{L}$  with high probability. This finishes the proof.

Theorem 1 shows that minimize  $\mathcal{L}$  is beneficial to improving the generalization performance of model on testing samples when the test samples have a higher class-imbalance ratio than training samples. That is to say, if the model has a small training error, it can still achieve a small test error on more imbalanced samples with high probability. Now we briefly discuss the case that there is only the majority branch. It can be verified that

$$\mathbb{E}_{(x_u, y_u)} \left[ \mathcal{L}(\boldsymbol{x}_u, y_u) \right]$$

$$= p \mathbb{E}_{\boldsymbol{x}_+} \left[ \log \left( 1 + e^{-z_u(\boldsymbol{x}_+)} \right) \right] + (1 - p) \mathbb{E}_{\boldsymbol{x}_+, \boldsymbol{x}_-} \left[ \log \left( 1 + e^{z_u(\boldsymbol{x}_-)} \right) \right],$$

$$\mathbb{E}_{(x,y)} \left[ \mathcal{L}(\boldsymbol{x}, y) \right]$$

$$= p' \mathbb{E}_{\boldsymbol{x}_+} \left[ \log \left( 1 + e^{-z_u(\boldsymbol{x}_+)} \right) \right] + (1 - p') \mathbb{E}_{\boldsymbol{x}_-} \left[ \log \left( 1 + e^{z_u(\boldsymbol{x}_-)} \right) \right].$$

It can be found that minimizing  $\mathbb{E}_{(x_u,y_u)}$  is not necessarily guarantee to minimize  $\mathbb{E}_{(x,y)} [\mathcal{L}(x,y)]$ , due to p' < p and 1-p' > 1-p. Similar results can be obtained for the case that there is only the minority branch. Therefore, directly learning on the vanilla distribution or re-adjusted distribution do not guarantee to tackle the case that test sample are more imbalanced.

#### 4. Experiments

#### 4.1. Datasets and Metrics

**Datasets**. In experiments, we verify the effectiveness of our methods on a real-world transaction payment dataset from Tencent Wechat Group. Due to the need for confidentiality, the information about datasets is obscured. The training set is specially collected by Wechat Group, whose imbalance ratio is around a few tens. The training set was collected over a period of time. The test set contains 6 days of payment data, and we refer to them as Day1, Day2, Day3, Day4, Day5 and Day6. The test set is highly imbalanced, which is different from the setting of the majority of literature in computer vision (Zhou et al., 2020). The imbalance ratio of test set much exceeds that of training set and it may be up to millions. In our experiments, we will show the results of the six days and the average results. **Metrics**. We adopt the metrics  $P_{20000}$ ,  $A_{20000}$ ,  $P_{50000}$  and  $A_{50000}$ . Please refer to Section 2 for the detailed definitions.

# 4.2. Baselines

In this section, we introduce some **strong** baseline method in computer vision to overcome data imbalance, which are detailed below.

**Cross Entropy**. Cross entropy loss is the most used loss function for classification tasks, which easily suffers from data imbalance.

Focal Loss (Lin et al., 2017). Focal loss adopts modulating weights to the cross-entropy loss in order to focus learning on hard samples.

Mixup (Zhang et al., 2018). Mixup is a data-agnostic data augmentation method, which convexly combines random pairs of training data and their associated targets.

**CE-DRS and CE-DRW**. These methods do not use bi-lateral branches but adopt two-stage training. In the first stage, it uses cross entropy loss for representation learning; in the second stage, it adopts re-balance learning to overcome data imbalance. Following the previous literature (Cao et al., 2019), we use re-sampling (CE-DRS) and re-weighting (CE-DRW) to achieve re-balance in the second stage.

LDAM and LDAM-DRW (Cao et al., 2019). The label-distribution-aware margin loss (LDAM) encourages larger margins for minority classes to address class imbalance. The LDAM-DRW is the combination of LDAM and re-weighting, which trains network first with vanilla LDAM loss and then transitions to using LDAM loss with a re-weighting schedule.

Class-balanced Loss (Cui et al., 2019). The class-balanced loss is to re-weight loss inversely with the effective number of samples per class. We adopt class-balanced cross entropy loss (CB-CE) and class-balanced focal loss (CB-Focal).

**BBN** (Zhou et al., 2020). BBN is the most relevant to our work. BBN also adopts a bilateral-branch network with instance-uniform and class-revered sampler for representation learning and classifier learning. The key difference between our method and BBN is that the two branches of BBN apply the same network but the two branches of our method adopt two difference networks with the same network architecture.

The Variant Loss of the Above Methods for Increasing  $A_K$ . In order to improve  $A_K$ , we adopt the amount m as the coefficient of the loss function of the fraudulent payments for the above method, which is similar to Equation (9). We use "-A" to represent these variants. including Cross Entropy-A, Focal Loss-A, Mixup-A, CE-DRS-A, CE-DRW-A, LDAM-A, LDAM-DRW-A, CB-CE-A, CB-Focal-A and BBN-A.

### 4.3. Implementation Details

The experiments is implemented by TensorFlow. For fair comparisons, the base settings are the same for all methods. The mini-batch size is set to 512. The training epochs is set to 20. The architecture of MLPs is set to 2048-512-128-1 except LDAM and BBN. LDAM Loss and its variant adopt the architecture 2048-512-128-2. BBN and its variant adopt the architecture 2048-512-128-2 is used for sharing weights. We adopt Adam optimizer to train the MLP. The initial learning rate is 0.0001.

#### 4.4. The Effect of Our Method

In Tables 1 to 4, we show the performance comparisons between our methods and the baseline methods over Day1-Day4. Tables 1 and 3 show the performance comparisons between BiCo and the baseline methods without considering the amount of fraud payments.

Date	Day 1				Day 2			
Method	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$
Cross Entropy	21.8	10.9	30.8	18.2	41.9	36.7	49.6	45.7
Focal Loss	24.8	11.9	27.1	12.4	35.0	20.9	48.7	41.0
Mixup	18.0	9.2	28.6	23.1	40.2	31.6	51.3	<b>46.8</b>
CE-DRS	0.0	0.0	0.8	0.2	0.9	5.1	0.9	5.1
CE-DRW	22.6	11.8	30.8	18.7	36.8	30.4	47.0	42.5
LDAM	21.1	7.8	27.8	14.5	41.9	<b>41.8</b>	49.6	44.6
LDAM-DRW	20.3	10.5	25.6	12.3	38.5	25.7	44.4	31.3
CB-CE	18.8	15.0	26.3	22.7	30.8	17.7	43.6	37.5
CB-Focal	19.5	10.0	26.3	14.2	33.3	27.2	38.5	28.8
BBN	3.8	2.1	5.3	5.8	6.0	8.2	7.7	17.5
BiCo	25.6	15.9	32.3	20.2	29.1	27.1	<b>53.0</b>	45.4

Table 1: Performance comparisons between our methods and baselines with considering amount (Day1 - Day2). The best results are denoted by bold.

Table 2: Performance comparisons between our methods and baselines considering amount (Day1 - Day2). The best results are denoted by bold.

Date	Day 1				Day 2			
Method	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$
Cross Entropy-A	25.6	12.8	37.6	30.5	41.9	39.5	50.4	45.7
Focal Loss-A	26.3	12.3	32.3	20.5	43.6	36.1	53.0	47.0
Mixup-A	26.3	17.6	34.6	27.6	31.6	33.0	41.9	43.6
CE-DRS-A	4.5	1.9	8.3	4.2	0.0	0.0	0.0	0.0
CE-DRW-A	27.8	13.2	33.1	18.9	40.2	26.6	53.0	45.2
LDAM-A	21.8	14.4	33.8	24.0	40.2	38.2	51.3	46.4
LDAM-DRW-A	24.1	11.7	29.3	14.9	41.9	41.4	52.1	46.1
CB-CE-A	24.1	16.1	33.1	21.7	28.2	24.4	49.6	34.1
CB-Focal-A	22.6	16.6	30.8	19.4	30.8	22.2	42.7	32.6
BBN-A	6.0	13.7	9.8	21.0	2.6	8.9	6.0	14.5
BiCo	25.6	15.9	32.3	20.2	29.1	27.1	53.0	45.4
BiCo-A	31.6	27.3	<b>39.1</b>	33.3	30.8	39.0	47.9	51.1
TriCo	29.3	17.9	35.3	25.4	47.9	44.1	58.1	47.9

Tables 2 and 4 show the performance comparisons between our three methods and the baseline methods with considering the amount of fraud payments. In Table 5, the average experiment results are presented. The experiment results of Day5-Day6 are detailed in the supplementary. In Tables 5 to 7, the experiment results are the average of 6 Days.

In Tables 2 and 4, we can observe that BiCo, a method which also does not consider the money of fraudulent payments, obtains the best results in most cases. According to

Date	Day 3				Day 4			
Method	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$
Cross Entropy	17.9	9.7	25.9	19.2	12.2	6.5	21.6	11.6
Focal Loss	17.9	8.0	25.9	12.1	10.8	6.0	20.3	10.6
Mixup	11.6	5.5	26.8	16.3	10.8	4.2	29.7	15.5
CE-DRS	0.9	0.9	1.8	1.4	0.0	0.0	0.0	0.0
CE-DRW	18.8	8.9	27.7	14.4	12.2	7.3	25.7	13.8
LDAM	20.5	13.6	27.7	16.6	17.6	8.6	27.0	13.8
LDAM-DRW	17.0	9.3	31.2	18.7	24.3	13.0	27.0	14.6
CB-CE	21.4	<b>21.4</b>	32.1	28.3	18.9	10.1	21.6	11.3
CB-Focal	14.3	9.2	24.1	14.1	18.9	9.6	25.7	13.8
BBN	3.6	4.7	3.6	4.7	2.7	2.6	4.1	3.1
BiCo	27.7	13.7	41.1	17.7	24.3	13.6	40.5	26.2

Table 3: Performance comparisons between our methods and baselines with considering amount (Day3 - Day4). The best results are denoted by bold.

Table 4: Performance comparisons between our methods and baselines without considering amount (Day3 - Day4). The best results are denoted by bold.

Date	Day 3				Day 4			
Method	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$
Cross Entropy-A	15.2	9.8	22.3	13.7	14.9	9.6	18.9	12.3
Focal Loss-A	15.2	10.1	27.7	16.1	12.2	6.9	16.2	9.6
Mixup-A	17.9	16.7	23.2	19.4	12.2	7.6	17.6	10.7
CE-DRS-A	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
CE-DRW-A	15.2	10.3	33.0	18.1	10.8	7.0	21.6	12.0
LDAM-A	14.3	7.0	25.0	15.0	8.1	4.5	25.7	13.6
LDAM-DRW-A	13.4	8.7	24.1	13.1	17.6	8.3	21.6	11.1
CB-CE-A	14.3	10.2	22.3	12.9	10.8	6.8	23.0	16.2
CB-Focal-A	9.8	5.0	17.9	8.9	9.5	6.4	14.9	9.1
BBN-A	0.0	0.0	10.7	22.4	1.4	0.8	5.4	7.2
BiCo	27.7	13.7	41.1	17.7	24.3	13.6	40.5	26.2
BiCo-A	25.0	<b>20.1</b>	<b>45.5</b>	<b>50.8</b>	14.9	14.5	20.3	18.1
TriCo	<b>30.4</b>	16.6	<b>45.5</b>	23.9	24.3	13.9	32.4	17.4

Table 5, BiCo outperforms the baseline methods without considering the money of fraudulent payments with a significant margin. We can also observe that these strong baselines in computer vision have very limited improvement or even worse performance compared to the performance of Cross Entropy. It means that compared to image data, the real-world payment data have many different characteristics including the extreme high imbalance of the test data and the tabular form in which the payments present, leading to ineffectiveness of the methods in computer vision. Note that the BBN method similar to BiCo also has

	Average Results					
Method	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$		
Cross Entropy	21.8	16.8	32.3	26.5		
Cross Entropy-A	22.6	19.8	32.7	32.0		
Focal Loss	20.0	13.6	29.4	22.6		
Focal Loss-A	22.1	16.9	31.7	25.2		
Mixup	18.2	15.4	30.8	26.9		
Mixup-A	20.7	18.2	30.7	30.7		
CE-DRS	0.3	1.0	0.7	1.2		
CE-DRS-A	0.8	0.3	1.6	0.8		
CE-DRW	21.6	16.3	33.7	25.7		
CE-DRW-A	22.7	18.6	35.3	27.9		
LDAM	23.6	21.1	33.6	30.0		
LDAM-A	19.4	16.0	31.7	24.9		
LDAM-DRW	23.0	13.7	32.3	24.1		
LDAM-DRW-A	22.1	17.8	29.7	22.7		
CB-CE	21.9	20.8	31.0	28.7		
CB-CE-A	19.1	16.8	32.5	28.2		
CB-Focal	20.7	17.3	30.4	26.3		
CB-Focal-A	16.7	13.9	26.3	21.6		
BBN	4.2	4.9	5.9	9.5		
BBN-A	4.2	10.2	9.6	19.9		
BiCo	27.7	19.8	43.9	30.5		
BiCo-A	27.1	<b>33.0</b>	39.7	45.9		
TriCo	32.3	25.0	<b>45.5</b>	34.8		

Table 5: Performance comparisons between ours methods and baseline methods (Average of Day1 - Day 6). The best results are denoted by bold.

very poor performance, which is probably due to the operation of sharing weights. MLP does not have the same powerful performance in tabular data as performance of Convolutional neural network (CNN) in image data. We provide more discussions and experiments in our ablation study to further investigate the difference between our methods and BBN.

In Tables 2 and 4, we compare our three methods with the baseline methods while considering the amount of the fraudulent payments. We can observe that our methods have the best performance in most cases. In Table 5, both BiCo-A and TriCo outperform the baseline methods with considering the money of fraudulent payments in all metrics. Combined with Table 1 and Table 2 or Table 3 and Table 4, we can observe that considering the amount of the fraudulent payments, i.e., adopting the amount as the coefficient of the loss of the fraudulent payments like Equation (9), help increase  $A_{20000}$  and  $A_{50000}$ , which means that the networks have greater capability of identifying the fraudulent payments with high amount. In Table 5, we can observe that directly replacing the normal cross entropy loss with Equation (9), *i.e.*, BiCo-A, can increase  $A_{20000}$  and  $A_{50000}$ , but it undermines

$\alpha$	Method	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$
0.5	BiCo	27.7	19.8	43.9	30.5
	BBN	10.9	11.1	14.6	13.2
$P_{ota}(0, 2, 0, 2)$	BiCo	30.1	21.9	43.5	32.4
Beta(0.2, 0.2)	BBN	7.7	7.0	12.8	10.8
$(rac{t}{T_{max}})^2$	BiCo	25.5	14.3	40.2	23.7
	BBN	4.1	4.4	5.1	4.8
$1 - \frac{t}{T_{max}}$	BiCo	28.5	21.8	41.6	33.6
	BBN	19.4	13.4	24.0	16.9
$cos(rac{t}{T_{max}}\cdotrac{\pi}{2})$	BiCo	30.1	21.1	39.4	26.3
	BBN	4.3	5.3	8.1	9.1
$1 - (\frac{t}{T_{max}})^2$	BiCo	25.9	18.8	40.2	26.8
	BBN	4.5	7.0	6.7	8.5

Table 6: Performance comparisons between BiCo and BBN under different adaptor strategies (Average of Day1 - Day6).

Table 7: Performance comparisons between TriCo and TriCo-CR (Average of Day1 - Day6).

Method	$P_{20000}$	$A_{20000}$	$P_{50000}$	$A_{50000}$
TriCo	32.3	25.0	45.5	34.8
TriCo-CR	28.5	27.9	42.9	41.7

 $P_{20000}$  and  $P_{50000}$ . TriCo, the method with trilateral branch framework, can help increase  $A_{20000}$  and  $A_{50000}$  and not undermine  $P_{20000}$  and  $P_{50000}$ .

# 5. Ablation study

### 5.1. More Study about BiCo and BBN

The BBN method (Zhou et al., 2020) seems similar to BiCo (ours). BiCo and BBN both use instance-uniform data sampler and class-reversed data sampler, and both employ the bi-lateral branch framework. In BiCo and BBN, the branch with instance-uniform data sampler both aims to achieve representation learning based on the original characteristic of the training data; the branch with class-revered data sampler both aim to overcome the high imbalance. For BBN, its loss function is formulated as

$$\mathcal{L} = \alpha l_{upper} + (1 - \alpha) l_{lower},$$

where  $\alpha$  is a trade-off between  $l_{upper}$  and  $l_{lower}$ , and BBN adopts a parabolic decay strategies  $\alpha = 1 - (\frac{t}{T_{max}})^2$  to adjust  $\alpha$ . According to paper proposed BBN method (Zhou et al., 2020), it investigates different adaptor strategies to adjust  $\alpha$  dynamically. Thus, we also investigate these strategies on BiCo and BBN. As shown in Table 6. We present the comparisons between Bico and BBN on six different adaptors strategies. We can observe that BiCo outperforms BBN under all six different strategies with significant margins. BBN has very

poor performance under all six adaptor strategies compared to Cross Entropy from Table 5. However, BiCo performs well under all conditions. Thus, the reason why BBN perform poorly but BiCo performs well is that MLP do not have the powerful capability to capture representation information and re-balanced information in one network in tabular data as CNN in image data. Thus, the operation of sharing weights in BBN makes it suffer from serious performance degradation.

# 5.2. More about Tri-collaborative Framework

The extra middle branch in Figure 2 adopts the cross-entropy considering the amount of the fraudulent payments and it applies the instance-uniform data sampler. In this section, we investigate the middle branch with class-revered data sampler, and we term such tricollaborative learning framework TriCo-CR. As shown in Table 7, we can observe that TriCo-CR also performs well. For  $P_{20000}$  and  $P_{50000}$ , TriCo performs better than TriCO-CR. In contrast, for  $A_{20000}$  and  $P_{50000}$ , TriCo-CR outperforms TriCo. The extra middle branch of TriCo considers instance-uniform data, which can help improve the representation ability, and thus improve the capability of identifying fraudulent payments. The extra middle branch of TriCo-CR considers class-reversed data sampler where fraudulent payments dominate the mini-batch, and mainly cares about the fraudulent payments with high amount. Thus, TriCo-CR has high value of  $A_{20000}$  and  $A_{50000}$ .

# 6. Conclusion

In this paper, we propose a simple and effective model to detect fraudulent transactions in electronic mobile and online payment platforms. With the key insight that decoupling the representation learning of majority and minority samples, our framework contains parallel branches with individual parameters to learn representations for majority and minority samples. Besides, we additionally add a loss re-weighted by amount to improve the recall amount of detected fraudulent transactions. Theoretical analysis shows that the proposed framework is applicable in the scenarios where test samples have a higher class-imbalanced ratio. Experiments on real-world datasets show that the proposed framework surpasses competitive methods. Our future work includes deploying the proposed framework at Wechat payment platform and exploring how to apply it on graph-structured data.

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